Integrating computation into the mechanistic hierarchy in the cognitive and neural sciences

Lotem Elber-Dorozko and Oron Shagrir

Abstract: It is generally accepted that, in the cognitive sciences, there are both computational and mechanistic explanations. We ask how computational explanations can integrate into the mechanistic hierarchy. The problem stems from the fact that implementation and mechanistic relations have different forms. The implementation relation, from the states of an abstract computational system (e.g., an automaton) to the physical, implementing states is a homomorphism mapping relation. The mechanistic relation, however, is that of part/whole; the explanans in a mechanistic explanation are components of the explanandum phenomenon. Moreover, each component in one level of mechanism is constituted and explained by components of an underlying level of mechanism. Hence, it seems, computational variables and functions cannot be mechanistically explained by the mediumdependent properties that implement them. How then, do the computational and implementational properties integrate to create the mechanistic hierarchy? After explicating the general problem (section 2), we further demonstrate it through a concrete example, of reinforcement learning, in cognitive neuroscience (sections 3 and 4). We then examine two possible solutions (section 5). On one solution, the mechanistic hierarchy embeds at the same levels computational and implementational properties. This picture fits with the view that computational explanations are mechanism sketches. On the other solution, there are two separate hierarchies, one computational and another implementational, which are related by the implementation relation. This picture fits with the view that computational explanations are functional and autonomous explanations. It is less clear how these solutions fit with the view that computational explanations are full-fledged mechanistic explanations. Finally, we argue that both pictures are consistent with the reinforcement learning example, but that scientific practice does not align with the view that computational models are merely mechanistic sketches (section 6).

1 1. Introduction

2 The question of how different explanations in the cognitive sciences relate to each other is widely debated (Kaplan and Craver, 2011; Piccinini and Craver, 2011; 3 Piccinini, 2015; Shapiro, 2017). We focus here on the relations between mechanistic 4 5 explanations and computational explanations in the neuro-cognitive sciences. 6 Mechanistic models describe the phenomenon's underlying mechanism. Often, they are considered explanatory because they describe a relevant causal structure, 7 namely, the causal structure that underlies the explanandum. Moreover, there is a 8 hierarchy of mechanistic explanations - each component in a mechanistic 9 explanation is itself explained mechanistically. Computational explanations are 10 similar to mathematical explanations in that they describe phenomena in abstract -11 mathematical or formal – terms. Computational explanations, however, are abstract 12 in a further sense. They arguably describe abstract, "medium-independent", 13 14 features. Thus, in computational explanations both the describing terms and the described objects/properties are abstract. 15

Several authors have recently suggested that computational explanations are a 16 species of mechanistic explanation (Kaplan, 2011; Kaplan and Craver, 2011; Piccinini 17 and Craver, 2011; Milkowski, 2013; Piccinini, 2015; Boone and Piccinini, 2016; Coelho 18 Mollo, 2018; Dewhurst, 2018). The focus of most of these accounts is the neuro-19 20 cognitive sciences, in which computational models and explanations are central to 21 the scientific investigation. Though the accounts are different in detail, they all share the starting point that computational explanations are in some sense abstract, 22 23 whereas mechanistic explanations describe causal relations between physical entities. Each account offers a unique way to bridge the apparent disparity between 24 computational and mechanistic explanations. 25

Whether computational models are indeed mechanistic is still under controversy (Huneman, 2010; Piccinini and Craver, 2011; Weiskopf, 2011; Kaplan, 2011; Kaplan and Craver, 2011; Lange, 2013; Chirimuuta, 2014, 2018; Bechtel and Shagrir, 2015; Rathkopf, 2015; Craver, 2016; Shagrir and Bechtel, 2017; Shapiro, 2017; Craver and Povich, 2017; Egan, 2017). Here we do not focus on this controversy (though our 31 analysis might have some implications regarding the nature of computation). Our concern is with the integration of computation – mechanistic or not – within the 32 hierarchy of mechanistic explanations. The concern arises from the disparity 33 34 between the implementation (or realization) relation and the explanans-35 explanandum relation in mechanistic explanations. The implementation relation 36 from the states of an abstract computational system (e.g., an automaton) to the 37 states of its implementing physical system is a homomorphism mapping relation, so 38 that each distinct computational state is mapped onto a distinct physical state, which 39 realizes it. The mechanistic relation, however, is that of part/whole. The explanans in 40 a mechanistic explanation are components of the explanandum phenomenon. 41 Moreover, each component in one level of mechanism is constituted and explained 42 by components of another, underlying, level of mechanism. Hence, it seems, 43 computational states are realized in some physical structures, but they do not stand 44 in part/whole relations to them and therefore they cannot be mechanistically 45 explained by the same structures. So, the question is: how do computational states integrate with implementational states to form the mechanistic hierarchy? 46

Before turning to address this question, we want to describe the main features of 47 48 mechanistic and computational explanations. Mechanistic explanations have three 49 main features: they are causal, decompositional and hierarchical. They are causal in 50 that they explain phenomena by describing their underlying mechanism. Consider 51 the reflex that is responsible for keeping the direction of gaze constant when the 52 head is rotated horizontally. It is called the horizontal vestibulo-ocular reflex. Its 53 function is explained by reference to an underlying mechanism whose inputs are the effects of head movements on the vestibular organ and whose outputs are given to 54 the ocular muscles. Within the mechanism there are feedforward inhibitory and 55 excitatory synaptic connections, so that each pre-synaptic neuron causally affects 56 57 the post-synaptic neurons through the synaptic connections (Kandel et al., 2013, chap. 40). Mechanistic explanations are decompositional because the explanandum 58 59 phenomenon is explained in terms of its components, their organization and their 60 activities (functions). In our example the constant gaze when the head is rotated is 61 explained by appeal to the specific synaptic connections between neurons, as well as

the neurons' change in firing rate in response to their synaptic inputs. Finally, mechanistic explanations are hierarchical: each explaining component in one level is itself the explanandum for another level of mechanism. Accordingly, the release of neurotransmitter to the synapse by the pre-synaptic neuron, is also explained mechanistically (see (Piccinini and Craver, 2011)). Our focus here is the third feature of mechanistic explanations, namely, the mechanistic hierarchy. An important point about the hierarchy is that each level in the hierarchy is a mechanistic explanation.

Computational explanations are taken to be abstract in that they refer to abstract, 69 "medium-independent", properties. This claim is fairly uncontroversial.¹ What 70 perhaps is more controversial is the claim that computational explanations refer only 71 to abstract, formal properties. Some authors argue that computational explanations 72 also refer to semantic properties, namely to the specific content of the states 73 (Shagrir, 2006; Sprevak, 2010); others might insist that computational explanations 74 75 also refer to some implementational, medium-dependent, properties (Some of the writings of (Kaplan, 2011, 2017; Dewhurst, 2018) may be interpreted this way). We 76 77 will not get into the debate about the nature of physical computation. Our concern is with the integration of abstract states and properties of computation in the 78 79 mechanistic hierarchy². We take abstract here to mean 'medium-independent' in the 80 sense that they can be implemented in very different physical media (e.g., both in brains and in computers). We will refer to these states and properties as 81 82 computational. But by this we assume in no way that computational states and 83 processes are only abstract.

84

¹ There are, however, different ways to account for the nature of these "medium-independent" properties. Fodor (1975) and Stich (1983) describe them as "syntactic" properties, and Fodor (1994) accounts for the latter in terms of high-level physical properties. Haugeland (1981) describes them as "formal" (see also (Fodor, 1980)). Piccinini (2015) describes computational properties as "mathematical" or "formal", and others have suggested that, regarding computations, the relevant physical properties of the implementing physical systems are only their degrees of freedom (Piccinini and Bahar, 2013; Coelho Mollo, 2018).

² While it seems straightforward to associate the computational explanations discussed here with Marr's computational level (1982), algorithmic descriptions of a system can also be abstract and computational in the meaning we discuss here, as long as they are 'medium-independent'. These algorithmic descriptions are more similar to mechanistic explanations in that they usually decompose the explanandum into its parts, while computational level explanations describe 'what' function the system performs and 'why' (Shagrir and Bechtel, 2017).

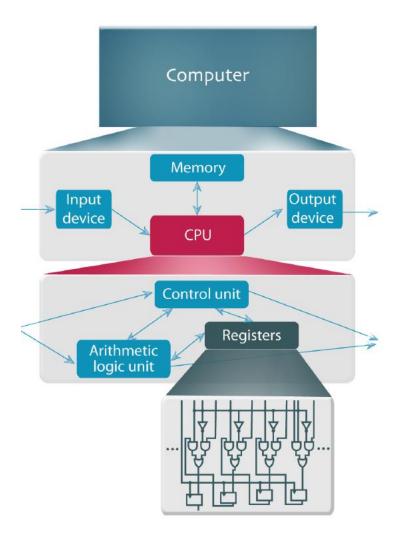
85 2. The computational and implementational hierarchies

Let us turn to the problem of integrating computational states and properties within the mechanistic hierarchy. As a warm-up, let us look at the way Piccinini describes this integration. Piccinini (2015), who defends the view that computational explanations are mechanistic, takes those computational levels to be levels of mechanism. In a crucial paragraph in his book he says the following:

91 The mechanistic account flows naturally from these theses. Computing systems, such as calculators and computers, consist of component parts 92 (processors, memory units, input devices, and output devices), their function 93 and organization. Those components also consist of component parts (e.g., 94 registers and circuits), their function, and their organization. Those, in turn, 95 consist of primitive computing components (paradigmatically, logic gates), 96 97 their functions, and their organization. Primitive computing components can be further analyzed mechanistically but not computationally (2015, pp. 118-98 119). 99

100 Now, we think that it is uncontroversial that Piccinini describes here levels of 101 computation that relate to each other in a part/whole relation. As Piccinini depicts it, 102 computers consist of processors, memory etc., which in turn consist of registers and 103 circuits, which in turn consist of logic gates (figure 1).

104 Figure 1 – The computational hierarchy



105

106 However, Piccinini does make a controversial claim, namely that computational 107 explanations are mechanistic. This claim has been criticized on three main grounds. Some critics argue that, even if some computational explanations are 108 109 decompositional as in the described case, there are other cases in which computational explanations do not decompose the explananda into components, 110 but instead refer to general structural or topological properties of the system, and so 111 are not mechanistic (Huneman, 2010; Rathkopf, 2015; but see Craver, 2016). A 112 second criticism is that computational explanations do not always aim to reveal 113 114 causal structures. Egan (2017) suggests that computational models are explanatory 115 because they are abstract and normative. Chirimuuta (2014) suggests that some computational models explain why a computation takes place by appeal to efficient 116 coding principles, and Shagrir and Bechtel suggest that some computational models 117 also explain the existence of a computation by appeal to environmental constraints 118

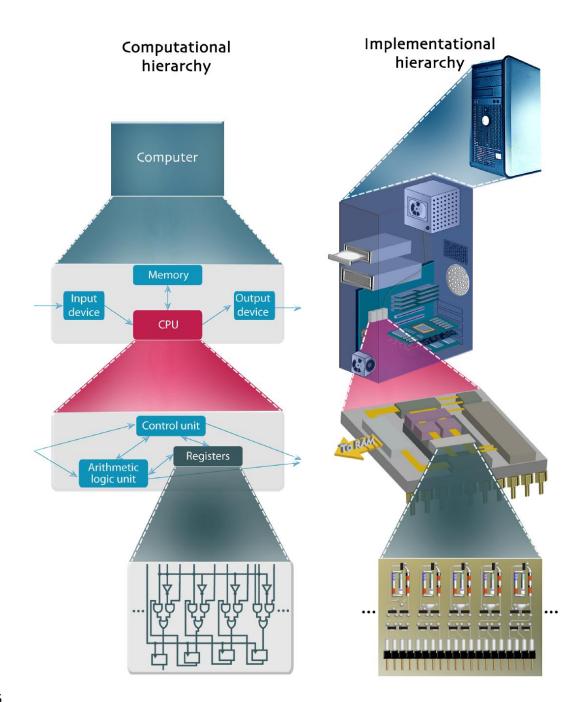
(Bechtel and Shagrir, 2015; Shagrir and Bechtel, 2017). According to these two
criticisms, computational explanations are not wholly mechanistic, but it still may be
that some computational explanations, which refer to medium-independent
properties, are decompositional, and therefore may be mechanistic.

123 Other critics argue that, even when computational explanations involve 124 decomposition, the resulting levels of computation are not levels of mechanisms. Instead, they argue that these levels are functional; they are part of a functional 125 analysis which explains the capacity (Fodor, 1968; Cummins, 1983, 2000). These 126 127 critics would agree that the levels are decompositional, relating to each other in a part/whole fashion, which is perfectly consistent with the functional account of 128 computational explanations. They would also agree that the pertinent computational 129 properties are "medium-independent", at least in the sense that they refer to 130 abstract and not to medium-dependent, implementational, properties. The critics 131 132 would argue, however, that the divide between the abstract/medium-independent properties and implementational properties is indicative of the divide between 133 134 functional and mechanistic explanations (Weiskopf, 2011; Shapiro, 2017). Because functional and implementational entities are inherently different, computational and 135 136 mechanistic explanations take place in different levels of explanation. Piccinini 137 (2015) in turn rejects the functional/mechanistic distinction, arguing that functional explanations are sketches of mechanism (Piccinini and Craver, 2011). Moreover, he 138 139 argues that computational explanations are (ideally) both abstract and full-fledged 140 mechanistic. They are abstract in the sense that they refer to medium-independent 141 properties. They are mechanistic in the sense that the medium-independent properties constrain the implementation ((Piccinini, 2015) But see Shapiro (2017) for 142 143 criticism).

We put aside the question of whether the computational level – as a level of abstract, medium-independent, properties – sufficiently constrains implementation to be considered mechanistic. We want to highlight a different issue that Piccinini and others do not discuss, namely, the way that computational (mediumindependent) and implementational (medium-dependent) properties relate to each other in the mechanistic hierarchy. 150 The picture depicted by Piccinini raises two (related) issues. The first pertains to the primitive computing components. Piccinini says that "primitive computing 151 components can be further analyzed mechanistically but not computationally". He 152 153 means that we can further analyze the logic gates in terms of non-computational, medium-dependent properties. The difficulty is that the logic gates are also 154 155 implemented in some medium-dependent properties. The inputs and outputs of 156 logic gates – typically characterized as 1s and 0s – are often implemented in systems with specific voltages. The implementing physical objects with specific voltages, 157 158 however, are not *parts* of the digits. More generally, implementation is often 159 characterized as a mapping homomorphism relation from the states of an abstract 160 computing system (e.g., an automaton) to groups of states of a physical system. For 161 example, there is a mapping from the digits 0 and 1 to the sets of voltages, 0-5 volts 162 and 5-10 volts. The sets of voltages, however, are not themselves the mechanism 163 that constitute the digits. The question raised, then, is about the relations between 164 the medium-independent properties that analyze computation in the mechanistic explanation and the medium-dependent properties that implement computation. 165 The first ones, the analyzing properties, seem to be parts of the digits, whereas the 166 167 second ones, the implementing properties, are not. Are these the same properties and how do they relate to each other? We expect a part-whole mechanistic analysis, 168 but we can only find in this stage an implementation-relation and not a part-whole 169 170 relation, so how can logic gates be explained mechanistically?

171 A second issue concerns the non-primitive computing components. The components 172 of a higher-level computation are analyzed by an underlying computational level. But they are also implemented in some medium-dependent properties. How are these 173 underlying properties – the computational and implementational – related? Take the 174 computational level that consists of "component parts (e.g., registers and circuits), 175 176 their function, and their organization". Let us call it C_n. The components of C_n can be analyzed, computationally, by the computational components of an underlying 177 178 computational level Cn-1 (e.g., logic gates). However, the computational components 179 of C_n are also implemented in some medium-dependent properties that belong to some mechanistic level, Pk. But how are Pk and Cn-1 related in the mechanistic 180

- 181 hierarchy? Moreover, P_k itself is part of a hierarchy, P_0 , P_1 , P_2 ,... So, there are two
- 182 hierarchies, one computational, C₁, C₂,... and one implementational, P₀, P₁, P₂,...
- 183 (figure 2).
- 184
- 185 Figure 2 The computational and implementational hierarchies



Several issues are worthwhile addressing regarding this picture. First, in some cases computational explanations are not decompositional (Huneman, 2010; Chirimuuta, 2014; Bechtel and Shagrir, 2015; Rathkopf, 2015; Egan, 2017; Shagrir and Bechtel, 2017), and therefore are not hierarchical. Although in such cases we will not find two or more hierarchies, the question of how the single-level computational explanation is integrated into the implementational hierarchy persists.

We would also like to note that much of the structure of these two hierarchies and 193 their relations depends on how one defines 'a level of explanation'. There is 194 195 practically unanimous agreement that in the scientific investigation of cognitive capacities both the underlying computation and the underlying implementation 196 should be addressed eventually. The question that is under debate addresses the 197 relevant details for a complete explanation of a capacity at a specific level. According 198 199 to the mechanistic framework, a complete explanation at each level will include all 200 the causally relevant relations and activities that constitute the explanandum 201 capacity.

Our question then is how the computational, medium-independent properties and their implementational, medium-dependent, properties relate to each other in the scientific explanation.³ Do we really find two hierarchies, one computational and one implementational, in which each level in each hierarchy is a complete explanation? And if this is indeed the case, then how do the two hierarchies relate to each other?

207 3. A hierarchical computational model for reinforcement learning

It could be argued that the two hierarchies we describe in the decomposition of the computer are the result of a specific man-made design, and that the observations from a computer cannot be generalized to the cognitive sciences. For this reason, it

³ One can also ask how the implementational hierarchy is decomposed. Depending on one's view of a level of explanation, the implementational hierarchy will include different details. It can include merely a reference to the physical structures that underlie the computational function. Alternatively, this hierarchy can also describe functions executed by these structures, albeit, medium-dependent functions. To illustrate, diodes, which are used on occasion to build logic gates in computers, have the function of passing electric current in exactly one direction. Description of such functions can be a part of the implementational hierarchy, because such functions are not abstract, but instead describe medium-dependent processes. In both cases the decomposition of the implementational hierarchy will depend on some function, in the first case it is the computational function, and in the second it is the medium-dependent function (which may or may not coincide with the computational function).

is useful to examine the relation between computation and implementation in themechanistic hierarchy with the help of an example from neuro-cognitive science.

213 Reinforcement learning is a behavior in which the subject learns to choose specific actions according to their consequences, with the goal of maximizing rewards. It is 214 215 widely investigated; it has received attention both from computer scientists who 216 have suggested algorithms for action selection that maximize specific outcomes 217 (Sutton and Barto, 1998), and from neural and cognitive scientists who have compared various reinforcement learning models with subjects' behaviors (Mongillo, 218 219 Shteingart and Loewenstein, 2014; Shteingart and Loewenstein, 2014) and searched for neural correlates of variables from reinforcement learning algorithms (Samejima 220 et al., 2005; Li and Daw, 2011; Wang, Miura and Uchida, 2013). 221

Reinforcement learning is a process that requires multiple different computations, and as such it can be viewed hierarchically. At the highest level, reinforcement learning is divided into four main processes, each involving its own computations: recognizing the subject's state, evaluating potential actions, selecting an action, and reevaluating the action based on the outcome (Doya, 2008).

Each one of these processes has been discussed in large bodies of literature and can 227 228 be further decomposed in various ways. To provide more concrete examples we will 229 discuss reinforcement learning in the context of a multi-armed bandit task, where there is only one state in which the subject repeatedly chooses between multiple 230 231 actions, each associated with a certain magnitude and probability of reward. We 232 describe here a simple and widely used algorithm for reinforcement learning, which 233 is called Q-learning (because the values associated with the actions are called Qvalues) (Sutton and Barto, 1998). In a multi-armed bandit task, reinforcement 234 235 learning has two main modules (instead of the four we originally mentioned), action 236 reevaluation and action selection.

237 Consider the module which is responsible for reevaluating an action after an 238 outcome. In Q-learning, each Q-value is meant to reflect the expected reward 239 associated with each action, also called the action-value. In order to learn this 240 action-value, after each trial a variable called the reward prediction error (RPE) is computed. The RPE is the difference between the reward that was just received andthe current value of the chosen action:

for the chosen action
$$a_i \rightarrow RPE(t) = R(t) - V_i(t)$$
 (1)

244 Where R(t) is the reward given at time t, a_i is action i and $V_i(t)$ is the action-value 245 of action i at time t. Then, the value of the chosen action is updated by summing the 246 previous value with a magnitude that is proportional to the RPE. Written formally:

247
$$if a_i was chosen \to V_i (t+1) = V_i (t) + \alpha \cdot RPE(t)$$
$$if a_i was not chosen \to V_i (t+1) = V_i (t)$$
(2)

248 Where α is a parameter that indicates the learning rate. The larger α is, the more 249 weight recent trials are given at the expense of previous trials.

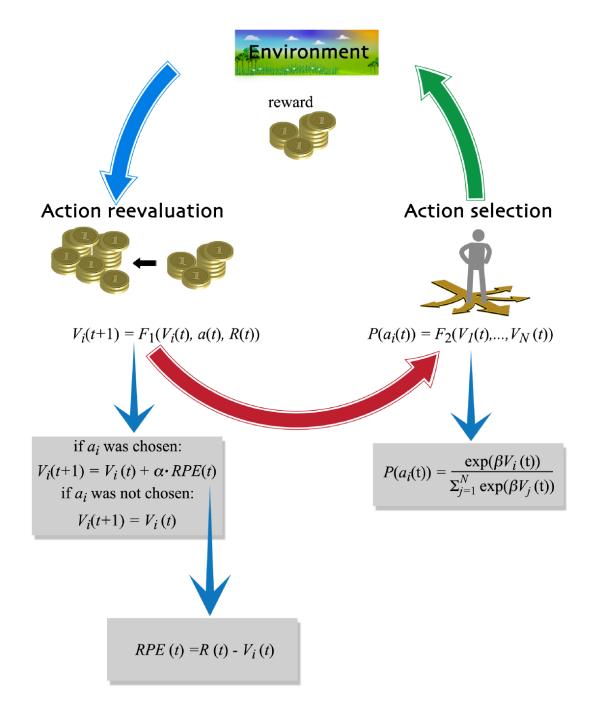
250 If we wish, we can continue this hierarchical computational explanation, by 251 explaining how the components in eq. (1)-(2) are computed. For example, we can 252 explain how the learning rate ' α ' is computed. We can also explain how the reward is 253 evaluated, or what the initial conditions set for $V_i(t = 0)$ are.

254 Consider now the second module, the module that is responsible for selecting 255 between different actions. The simplest kind of module would just select the action that has the highest value, according to the computation in eq. (2). However, this 256 method may never sample actions that initially received lower values, even in cases 257 where these lower values were underestimates of the true values. Therefore, it is 258 generally agreed that some form of exploration is required, i.e., actions with lower 259 values should be chosen with a non-zero probability. A common model that 260 261 incorporates exploration into the choice is a 'softmax' function where actions with 262 higher values have a higher probability to be chosen. The 'softmax' function is:

263
$$P(a_i(t)) = \frac{e^{\beta V_i(t)}}{\sum_{j=1}^n e^{\beta V_j(t)}} \quad (3)$$

264 Where a_i is action i, $P(a_i(t))$ is the probability of choosing action i at time t, $V_i(t)$ 265 is the action-value of action i at time t, n is the number of possible actions, and β is 266 a parameter that determines the bias of the choice towards the higher valued actions. The components of this action selection function can also be further explained. For example, in this equation, the choice is stochastic. We can also provide a model for this stochasticity. Or we can explain the choice of β , which may be a constant, or change throughout learning. Fig. 3 presents a summary of the hierarchical model we described so far.

272 Figure 3 The computational hierarchy of the Q-learning model



273

Using the two modules described above, in a multi-armed bandit task, in which subjects choose between several actions repeatedly, it is possible to learn to choose the action that is associated with the largest expected reward most frequently. Hence, a popular theory in the cognitive sciences is that people employ a model similar to Q-learning in various instances of reinforcement learning tasks.

279 Q-learning is not the only model that has been suggested for reinforcement learning, it has a few competitors at several different levels. First, some reinforcement 280 learning algorithms do not compute the values of actions at all. Instead, learning is 281 282 done directly on the 'policy': the probability of choosing each action. These are called direct-policy learning algorithms (Mongillo, Shteingart and Loewenstein, 2014; 283 Shteingart and Loewenstein, 2014). Second, in the Q-learning model the action 284 selection function (eq. 3) utilizes the same action-values as the action reevaluation 285 286 function (eq. 2). However, in some reinforcement learning algorithms, the action 287 selection function does not employ the action-value estimates of the action reevaluation function. Instead, the only signal the action-selection function receives 288 289 from the action-reevaluation function is the RPE. In these algorithms, these two modules are also called the 'actor' and the 'critic', respectively (Sutton and Barto, 290 291 1998). A third issue concerns the complexity of Q-learning. It is argued that it is too 292 simple to explain a wide variety of behaviors and therefore this original model has 293 been developed into alternative, more complicated models (Botvinick, Niv and Barto, 294 2009; Botvinick, 2012). Each of these three groups of competing models challenges a 295 different part of the computational hierarchy of Q-learning. The first group of 296 models challenges whether there is an action reevaluation function at all, the second 297 group of models questions the relation between the action selection and the action 298 reevaluation functions and the third presents alternatives to the structure within 299 each function.

We believe that the point is clear, the Q-learning model is hierarchical in nature. Furthermore, all properties discussed in the Q-learning model are mediumindependent: they do not necessitate a specific physical structure. In fact, they are abstract enough that they can be both implemented in computers and, as many scientists hypothesize, in brains (Schultz, Dayan and Montague, 1997; Doya, 2000,
2008; O'Doherty *et al.*, 2004; Samejima *et al.*, 2005).

306 4. The computational and implementational hierarchies of reinforcement learning

307 A great deal of scientific research has been dedicated to the characterization of the 308 neural correlates of the Q-learning model (Hollerman and Schultz, 1998; Doya, 2000, 309 2008; Samejima et al., 2005; Ito and Doya, 2009; Kable and Glimcher, 2009; Tai et al., 2012; Wang, Miura and Uchida, 2013). Experimental evidence has implicated the 310 basal ganglia, a group of several subcortical nuclei, including the striatum, pallidum 311 and substantia nigra, in decision making, and specifically in the context of 312 313 reinforcement learning (Doya, 2000). With regard to the different modules of reinforcement learning, the coding of state and possible actions in each state has 314 been attributed to the cortex, the calculation of the expected reward associated 315 316 with each action (action reevaluation) has been attributed to the striatum, action 317 selection has been attributed to the pallidum, etc. In Fig. 4 you can see a scientific hypothetical model which describes the implementation of the computational 318 319 modules in reinforcement learning.

Figure 4. The implementational model for reinforcement learning. Adopted from(Doya, 2008). Legend is taken from the original paper.

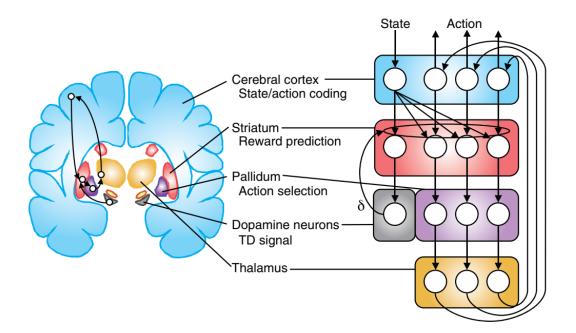


Figure 2 A hypothetical model of realization of reinforcement learning in the cortex–basal ganglia network². Left, coronal section of the brain. Right, functional model, where δ denotes the reward prediction error carried by the midbrain dopamine neurons.

322

The attribution of specific computational properties to brain areas corresponds to 323 their connectivity patterns. On the Q-learning model we expect action-values to play 324 325 a part in the action selection function (eq. 3). On our implementational model striatal neurons represent action-values and pallidal neurons are responsible for 326 action selection. Indeed, in line with the computational model, we see that striatal 327 neurons target and causally affect pallidal neurons. Hence, on this description, 328 329 abstract computational relations are translated into causal relations between physical brain areas.⁴ 330

One can wonder about the model on the right-hand side of Fig. 4. While the model on the left-hand side clearly describes causal relations between brain areas, the model on the right-hand side is abstract and is termed functional by (Doya, 2008). Although its drawing is abstract, this model is committed to specific brain areas, sometimes describing brain areas without an apparent function (such as the Thalamus). For this reason, it would be difficult to consider this model a functional analysis, as described by (Fodor, 1968; Cummins, 1983, 2000). Furthermore, this

⁴ Some may argue that relations between computational components can already be considered causal relations. We discuss the possible outcomes of this position in section 5.

338 model is committed to specific media, namely, brain areas, and therefore it does not 339 describe medium-independent properties. For this reason, we consider it an 340 implementational model. However, for those who believe that computational 341 models are both complete mechanistic explanations and medium-independent 342 (Piccinini, 2015), this model, which focuses on the abstract functions of specific brain 343 areas, may be similar to what they have in mind⁵.

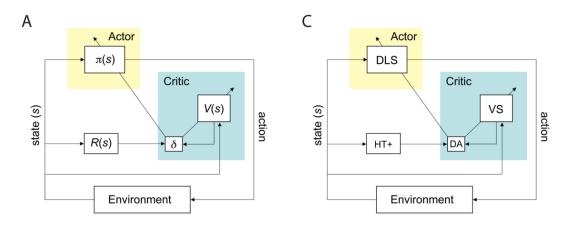
The components in the implementation described in Fig. 4 can be decomposed 344 themselves into subparts, which correspond to parts of the computations. For 345 346 example, there is experimental evidence that midbrain dopaminergic neurons that provide input to striatal neurons, encode the reward prediction error (RPE) (eq. 1), 347 which is a component in the calculation of action-values (eq. 2) (Schultz, Dayan and 348 Montague, 1997; Hollerman and Schultz, 1998). To provide another example, 349 350 neurons in both the ventral and dorsal striatum receive inputs from midbrain 351 dopamine neurons, which are taken to encode the RPE (note the arrow from the gray box to the red box in Fig. 4). Therefore, both are taken to play a role in reward 352 353 prediction. Experimental findings have suggested that neuronal activity in the striatum can be divided into two anatomically and functionally separate parts of 354 355 reward prediction: the dorsal striatum plays a role in associating stimuli with 356 responses, corresponding primarily to an 'actor' (action selection) module, while the ventral striatum plays a role in updating the predictions of future rewards expected 357 358 in each state, corresponding to a 'critic' (action reevaluation) module (O'Doherty et 359 al., 2004).

We see in this example two distinct hierarchies, one computational and one implementational. Parts of the computational hierarchy can be seen in Fig. 3. This hierarchy is abstract, medium-independent and can be discussed without mention of any brain structures. We can also see an implementational hierarchy, part of it is depicted in fig. 4, where brain structures are decomposed into functionally and anatomically individuated components. In some scientific publications we even see

⁵ If this is the case, some issues regarding this view should be resolved. Most importantly, how function can remain medium-independent when it is necessary to state the brain structure in which they occur (Haimovici, 2013).

366 computational and implementational models for decision making (albeit slightly367 different models from the Q-learning model) depicted side by side, as in Fig. 5.

Figure 5 Computational and implementational models, side by side. Adopted from (Botvinick, Niv and Barto, 2009). R(s): reward function; V(s): value function; δ : reward prediction error; π (s): policy (action-selection function). DA: dopamine; DLS, dorsolateral striatum; HT+: hypothalamus and other structures; VS, ventral striatum.



372

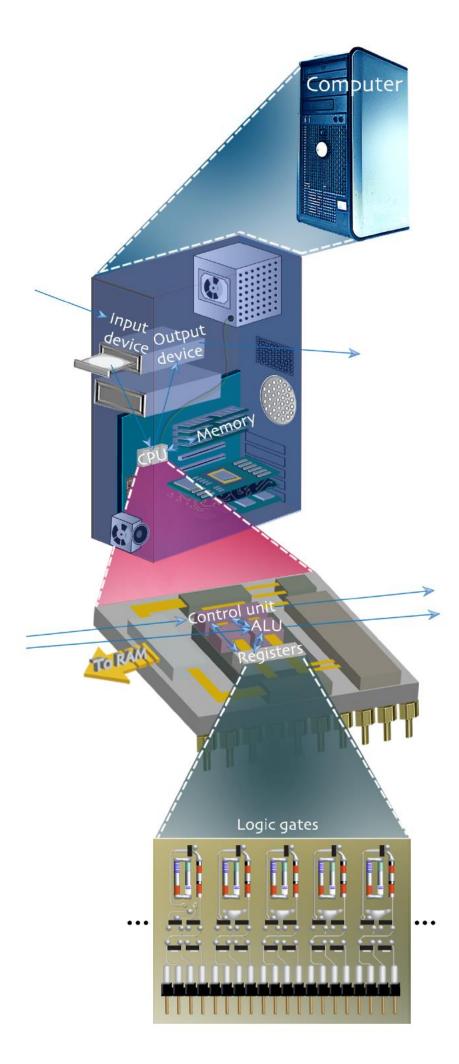
The relation between these two hierarchies is that of implementation, throughout the scientific literature brain structures are described as 'implementing' (Ito and Doya, 2011), 'realizing' (Doya, 2008), 'representing' (Samejima *et al.*, 2005) and 'encoding' (Schultz, Dayan and Montague, 1997) computational properties.

5. The relation between the computational and implementational hierarchies

We found in our scientific example two hierarchies, like the ones described in Fig. 2. 378 379 However, there are still many open questions about these hierarchies, both in 380 general and in our example. How do these hierarchies relate to each other within the 381 scientific explanation? How does this relation reflect the explanatory role of the 382 computational and implementational models? Finally, what role do implementation 383 relations and part/whole relations play in the explanation of cognitive phenomena? In this section, we suggest possible answers to these questions and investigate their 384 merit. We relate these possible answers to the different views about abstractness 385 386 and completeness of computational models. We do not aim to support one stance 387 on this question, but instead wish to examine the consequence of the different positions about computational models as explanations and start a debate about 388 389 these possible solutions.

We can think of two ways to relate computation and implementation to each other within the mechanistic hierarchy. One is lumping together the implementational and the abstract properties in each level, namely C1 and P1, C2 and P2 and so on. Figure 6 shows an example of this picture on the decomposition of a computer.

Figure 6 A single combined mechanistic hierarchy. Each level includes both abstract and implementational properties that are related through implementation. The implementational properties are denoted by the drawings in the figure, while the computational properties are denoted by the words and arrows appearing on top of the implementational properties.



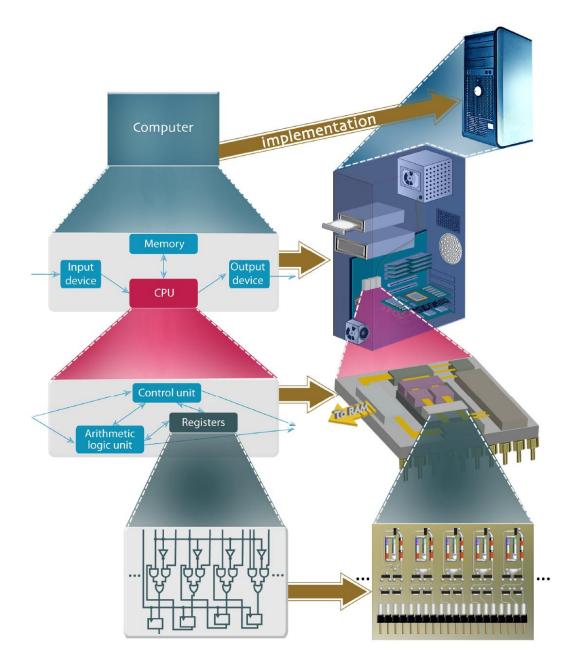
400 On this picture we do not really have two separate hierarchies, but only one: The 401 pertinent computational properties are lumped together with their 402 implementational properties in the same level(s) of explanation (a similar structure 403 of explanation is presented in (Harbecke, under review)). This simple solution implies 404 that computational and implementational properties figure together in the same 405 explanation and in the same levels of the mechanistic hierarchy. This solution is in 406 tension with the view that computational explanations are autonomous from implementation and therefore do not require implementation details to be 407 408 complete, but fits quite nicely with the picture on which computational explanations 409 are sketches of mechanisms (some people, e.g., (Rusanen and Lappi, 2016; Shagrir, 410 2016) interpret (Kaplan and Craver, 2011; Piccinini and Craver, 2011) as advocates of 411 this position). On this picture, the computational sketches turn into a full-fledged 412 mechanistic explanation only when we complement the sketches with the same-413 level implementational properties. When both kinds of properties are mentioned 414 then we have a full-fledged mechanistic explanation, hence a level of mechanism. The mechanistic hierarchy simply embeds within it, a sub-hierarchy of computational 415 sketches. 416

417 We can see two possible upshots of this construal, depending on one's view of 418 computational models as sketches. One may consider computational sketches to 419 simply be partial descriptions of the implementational model and computational 420 properties to simply be abstract facets of the implementing properties, stripped 421 away from their medium-dependent aspects. On this formulation, when the 422 implementing properties are described in an explanation, the computational properties, which are merely a part of the implementational properties, become 423 redundant. We are left with an implementational hierarchy, partial descriptions of 424 425 which are computational models. On such a view it is clear how there is only one mechanistic hierarchy - an implementational hierarchy. However, this view 426 completely dismisses any explanatory value of computational descriptions that goes 427 428 above implementational descriptions and some may argue that this is inconsistent 429 with scientific practice, which often appeals to computational explanations as more than partial implementational descriptions (Haimovici, 2013). Alternatively, one may 430

believe that computational sketches can include details and aspects which are not 431 part of the implementational model. For example, that they address environmental 432 433 constraints or efficient coding principles (Chirimuuta, 2014; Bechtel and Shagrir, 434 2015; Shagrir and Bechtel, 2017). Therefore, in the complete model both 435 computational and implementational properties figure together. This view takes 436 computational descriptions to be more than partial implementational descriptions, 437 but it brings up the original problem discussed in this paper - how the unique computational properties relate to the implementational properties in each level of 438 439 the hierarchy.

440 A second option is to keep the two hierarchies apart (figure 7). The two hierarchies are related through the implementation relation. The computational properties of 441 442 C1 are mapped (implemented by) to the implementational properties of P1, the 443 computational properties of C2 are mapped to the implementational properties of 444 P2, and so on. While objects by the same name may appear in both hierarchies, such as CPUs and registers in Fig. 7, the computational hierarchy includes only abstract, 445 446 medium-independent properties (e.g., digits in logic gates) and the implementational hierarchy includes physical, medium-dependent properties (e.g., voltages). Fig. 7 447 448 presents a simple case where each computational level is mapped to each 449 implementational level. In reality there might not be a perfect match between the 450 hierarchies and computational properties at the same level may be implemented in 451 implementational properties in different levels. However the structure of the 452 implementation relation, in all cases in this picture there are two hierarchies and the 453 computational properties in the computational hierarch are implemented by implementational properties in the implementational hierarchy. This solution is 454 more hospitable to the notion that there is multiple realization of cognitive 455 functions, since the same computational hierarchy can be related to (i.e., 456 457 implemented in) different implementational hierarchies.

Figure 7 Two separate hierarchies, one computational and one implementational,
that are related through implementation. Each level in each hierarchy is a complete
explanation of the phenomenon at the higher level.



461

462 This picture fits quite nicely with the functional view of explanation, namely, the idea that computational explanations are full-fledged functional (yet non-mechanistic) 463 explanations. According to this functional picture, computational explanations are 464 distinct and autonomous from mechanistic explanations (Fodor, 1968; Cummins, 465 1983), which fits with the solution in which the two hierarchies are distinct. 466 Computational and implementational properties do not figure together in the 467 decompositional explanation of the same capacities. Instead, only computational 468 properties are part of the decomposition of computations. Implementational 469 470 properties can still figure in explanations of computations, but these explanations

471 will not be mechanistic because there is no part/whole relation between explanans 472 and explanandum. While on this picture the two hierarchies are separate, they still 473 constrain each other: the relevant implementational properties are determined 474 according to the computational function, and the computational hierarchy must be 475 one which can be implemented in the physical system. Despite these mutual 476 constraints, those supporting this picture will argue that the computation performed as part of some cognitive capacity can be given a complete explanation at one level 477 without any reference to implementation and that the implementation details 478 479 explain a different aspect of this capacity, namely, how the capacity is implemented. 480 That is, computational and implementational explanations answer different 481 questions.

482 On both pictures, primitive computing processes are analyzed mechanistically, if at 483 all, only indirectly. The primitive computational components, e.g., logic gates, are 484 *implemented* in some implementational properties, e.g., voltages, whereas only the latter can be further analyzed mechanistically. On the combined-hierarchy picture 485 486 (Fig. 6), the computational properties will figure together with implementational 487 properties in each level, until at some point the primitive computing processes can 488 no longer be decomposed, and only implementational properties will continue to be 489 decomposed in the hierarchy. On the separate-hierarchies picture (Fig. 7), the 490 computational hierarchy will terminate at the primitive computing components.

491 On both pictures, the implementation is not a part/whole relation and therefore the 492 description of implementation cannot be taken as a mechanistic explanation. 493 Nonetheless, these two pictures do differ in how they view the role of implementation in explanation in general. On the combined picture, both 494 computational and implementational details figure together in one mechanistic 495 hierarchy. Therefore, it is natural to take relations of implementation to not have an 496 497 explanatory role. Instead, medium-dependent details are taken to explain by 498 decomposition of the phenomena. On the separate-hierarchies picture 499 implementation can be considered to have a non-mechanistic explanatory role: it 500 explains how the explanandum, as well as the computational hierarchy are 501 implemented (see (Coelho Mollo, 2018)).

What about the view that computational explanations are both abstract and full-502 fledged mechanistic explanations? It would be difficult to see how the first solution 503 in Fig. 6 can be consistent with it; if computational explanations are complete 504 505 mechanistic explanations why do they require additional implementation details in 506 the same mechanistic level of explanation? The second solution in Fig. 7 is not 507 necessarily inconsistent with this view. For example, if one takes computational 508 states and properties to have causal powers, then one can view the computational hierarchy as a hierarchy of complete mechanistic explanations. However, on this 509 510 view the role of the implementational hierarchy still needs to be explicated. A 511 possible implication is that the overall mechanistic picture is more complex: We have 512 different mechanistic hierarchies that apply to different properties of the same objects/components. But under this picture any computational capacity has at least 513 514 two hierarchical explanations, and it is not obvious which one of them should be 515 considered the mechanistic explanation. A possible way to elucidate this complex picture is to maintain that the implementational hierarchy explains how the 516 computational hierarchy is implemented, rather than how the cognitive capacity is 517 performed (Coelho Mollo, 2018). On this view, the computational hierarchy is the 518 519 mechanistic hierarchy which decomposes the cognitive capacity and the implementational hierarchy is an appendix which explain the implementation of the 520 521 computation.

522 **6. Some insights from reinforcement learning**

523 It can be useful to examine the relation between the hierarchies in reinforcement 524 learning. When considering the computational and implementational hierarchical models for reinforcement learning, which solution best describes the relation 525 between these hierarchies? We believe that evidence in this case is mixed and can 526 support both suggested solutions for the relation between the hierarchies. On the 527 528 picture seen on Fig. 6, each level combines computation and implementation into 529 one mechanistic explanation. Therefore, we would expect the scientific investigation of lower levels to include a physical decomposition of the higher level, as occurs in 530 mechanistic explanations. However, in our example the scientific investigation of the 531 implementation of the computational hierarchy searches for the implementation of 532

variables at various levels of this hierarchy, such as the representations of action-533 value (Samejima et al., 2005), RPE (Schultz, Dayan and Montague, 1997) and learning 534 rate (α in eq. 1) (Behrens *et al.*, 2007). Often, the search for a lower-level variable 535 536 such as the learning rate takes place in the absence of a scientifically supported 537 neural correlate for the higher level computational variable of which it consists (In 538 this case the calculation of action-value). Hence, the search for neural correlates 539 here is more akin to searching for relations between two separate computational and implementational hierarchies than to physically decomposing mechanisms. 540

541 Moreover, scientific investigation of both hierarchies can and has been conducted separately. The Q-learning algorithm for reinforcement learning has been 542 investigated both analytically (Watkins and Dayan, 1992) and behaviorally 543 (Shteingart, Neiman and Loewenstein, 2013). These methods ignore the neural 544 correlates of this model. Similarly, the basal ganglia have been investigated 545 546 anatomically and functionally without addressing computational models for reinforcement learning (Hoshi et al., 2005). This suggests that a framework of two 547 548 hierarchies, as presented in Fig. 7, is the appropriate one in this case.

549 On the other hand, it can be argued that current scientific research is still preliminary 550 and not indicative of the final form of a fully-fledged scientific explanation. Hints that 551 such a form will include one combined mechanistic hierarchy can be found in the 552 fact that scientific debates today about the plausibility of specific computational 553 models of reinforcement learning often also appeal to the plausibility of the 554 implementation of these models (Botvinick, Niv and Barto, 2009).

555 Moreover, findings of implementation of specific computational variables can be 556 used to support or refute abstract computational models. Recall the three challenges 557 to the computational model we presented in the section 3. The first one suggested 558 that instead of learning the values of the actions, there is 'direct-policy' learning 559 where the probability of choosing each action (i.e., the policy) is reevaluated at each 560 step. However, the finding that striatal neurons represent the expected reward 561 associated with each action (Samejima *et al.*, 2005) can be taken as support for the 562 hypothesis that a Q-learning model is implemented in the brain, rather than a 563 'direct-policy' model⁶.

The finding in (O'Doherty et al., 2004) that striatal neurons can be divided into 564 'actor' and 'critic' modules can be used as evidence in the second challenge: 565 566 whether the action selection and action reevaluation modules can be separated into 567 'actor' and 'critic'. It is also increasingly popular to suggest computational models 568 that are informed by the structure of neural networks, with the purpose of suggesting models that are more biologically plausible (Mnih et al., 2016). Note that, 569 570 even though physical structures are used as evidence in this debate, the questions pertain to the architecture of the abstract computational model, which can be 571 572 implemented both in computers and in brains.

Given these examples it can be argued that the practice of developing a complete explanation at each level of the explanatory hierarchy involves a close and reciprocal relation between the computational models and their possible implementation, and that computational models are not considered explanations until they have been shown to be implemented in the brain. This suggests that computation and implementation belong together in one level of the explanation. Therefore, the pictures presented in Figs. 6-7 are both still possible regarding this example.

580 However, when considering whether computational descriptions are merely sketches of mechanisms, on the interpretation of sketches as partial descriptions of 581 582 implementation, the evidence is more conclusive. We see that, in our example of reinforcement learning, evidence from scientific practice is strongly against the view 583 584 of computational models as sketches. Moreover, scientific practice tends to take implementational details to explain the implementation of the computational model 585 rather than the cognitive capacity directly. Often, when findings of neural correlates 586 587 of reinforcement learning models are reported, they are reported as discoveries about the implementation of these models. Hence, such findings are taken to 588 answer questions about how, and whether a specific computational model is 589 590 implemented in the brain and they do not attempt to explain reinforcement learning 591 (or decision making in general) without appeal to some computational model. Perhaps the strongest indication for this is in experiments where there is some 592 593 causal intervention on brain areas and behavioral changes are measured. If 594 computational models are merely partial descriptions of implementation, they will 595 be unnecessary in the interpretation of causal experiments, where the causal 596 structure is already described in the results of the experiment. However, often, 597 results in such experiments are interpreted in the framework of a computational model of reinforcement learning (Tai et al., 2012; Wang, Miura and Uchida, 2013; 598 599 Lee et al., 2015). For example, (Tai et al., 2012) find that stimulation of striatal 600 neurons causes a bias in choices, and they interpret these results by saying that 601 stimulation of striatal neurons mimics changes in action-value. Hence, instead of 602 utilizing the causal finding to explain the behavior of the subjects, (Tai et al., 2012) 603 use their finding as an indication of implementation of action-value – a 604 computational variable. Such a computational interpretation to causal results is 605 difficult to explain if computational models are taken to be merely partial descriptions of causal mechanisms and is much more in line with the view that 606 607 computational models have a unique explanatory value. Moreover, this scientific 608 practice can be taken to support the claim that implementational details are taken to explain the computational model rather than the cognitive capacity itself. 609

For this reason, we believe that our example does not support the view that computational models are partial descriptions or that computational models are explanatory only because they describe causal relations. Instead, this reinforcement learning example is more consistent with the view that computational properties play an invaluable role in the explanation of cognitive phenomena.

Nonetheless, reinforcement learning is just one example of computational models of
cognitive capacities. Future investigation of other computational models will be
telling regarding the relation between computation and implementation.

618 7 Conclusions

619 After raising the problem of how computational explanations integrate in the 620 mechanistic hierarchy, we analyzed reinforcement learning as an example of a

computational model in neuroscience and reviewed two possible pictures of the 621 relations between computation and implementation in the mechanistic hierarchy. 622 On the one-hierarchy picture computational and their implementational properties 623 624 reside in the same level(s) of explanation. On the two-hierarchy picture 625 computational and implementational properties reside in different computational 626 and implementational hierarchies. We concluded that both pictures are possible regarding the reinforcement learning example, but that scientific practice does not 627 align with the view that computational models are merely mechanistic sketches. 628

629 Bibliography

Bechtel, W. and Shagrir, O. (2015) 'The Non-Redundant Contributions of Marr's

- Three Levels of Analysis for Explaining Information-Processing Mechanisms', *Topics in Cognitive Science*, 7, pp. 312–322.
- Behrens, T. E. J. *et al.* (2007) 'Learning the value of information in an uncertain
 world', *Nature Neuroscience*, 10, pp. 1214–1221. doi: 10.1038/nn1954.
- Boone, W. and Piccinini, G. (2016) 'The cognitive neuroscience revolution', *Synthese*,
 193, pp. 1509–1534.
- Botvinick, M. M. (2012) 'Hierarchical reinforcement learning and decision making', *Current Opinion in Neurobiology*, 22, pp. 956–962. doi: 10.1016/j.conb.2012.05.008.

Botvinick, M., Niv, Y. and Barto, A. (2009) 'Hierarchically organized behavior and its
neural foundations: A reinforcement learning perspective', *Cognition*, 113, pp. 262–
280. doi: 10.1016/j.cognition.2008.08.011.Hierarchically.

- Chirimuuta, M. (2014) 'Minimal models and canonical neural computations: the
 distinctness of computational explanation in neuroscience', *Synthese*, 191, pp. 127–
 153.
- Chirimuuta, M. (2018) 'Explanation in Computational Neuroscience: Causal and Noncausal', *The British Journal for the Philosophy of Science*, 69, pp. 849–880. doi:
 10.1093/bjps/axw034.
- Coelho Mollo, D. (2018) 'Functional individuation, mechanistic implementation: the
 proper way of seeing the mechanistic view of concrete computation', *Synthese*, 195,
 pp. 3477–3497. doi: 10.1007/s11229-017-1380-5.
- 651 Craver, C. F. (2016) 'The Explanatory Power of Network Models', *Philosophy of*652 *Science*, 83, pp. 698–709.
- Craver, C. F. and Povich, M. (2017) 'The directionality of distinctively mathematical
 explanations', *Studies in History and Philosophy of Science*, 63, pp. 31–38. doi:
 10.1016/j.shpsa.2017.04.005.

- 656 Cummins, R. (1983) *The Nature of Psychological Explanation*. MIT Press.
- 657 Cummins, R. (2000) "How does it work?" vs. "What are the laws?" Two conceptions
 658 of psychological explanation.', in Keil, F. and Wilson, R. A. (eds) *Explanation and*659 *Cognition*. MIT Press, pp. 117–145.
- Dewhurst, J. (2018) 'Individuation without Representation', *The British Journal for the Philosophy of Science*, 69, pp. 103–116. doi: 10.1093/bjps/axw018.
- Doya, K. (2000) 'Complementary roles of basal ganglia and cerebellum in learning
 and motor control', *Current Opinion in Neurobiology*, 10, pp. 732–739. doi:
 10.1016/S0959-4388(00)00153-7.
- 665 Doya, K. (2008) 'Modulators of decision making', *Nature Neuroscience*, 11, pp. 410– 666 416. doi: 10.1038/nn2077.
- 667 Egan, F. (2017) 'Function-Theoretic Explanation and Neural Mechanisms', in Kaplan,
- D. M. (ed.) *Explanation and Integration in Mind and Brain Science*. Oxford University
 Press, pp. 145–163.
- Elber-Dorozko, L. and Loewenstein, Y. (2018) 'Striatal action-value neurons
 reconsidered', *eLife*, 7, p. e34248. doi: 10.7554/eLife.34248.
- Fodor, J. (1968) *Psychological Explanation: An Introduction To The Philosophy Of Psychology*. Random House.
- Fodor, J. (1980) 'Methodological solipsism considered as a research strategy in
 cognitive psychology', *Behavioral and Brain Sciences*, 3, pp. 63–73.
- Fodor, J. (1994) *The elm and the expert*. MIT Press.
- 677 Fodor, J. A. (1975) *The Language of Thought*. Harvard University Press.
- Haimovici, S. (2013) 'A Problem for the Mechanistic Account of Computation', *Journal of Cognitive Science*, 14, pp. 151–181.
- Harbecke, J. (under review) 'Multiple Level Hierarchies in Cognitive Neuroscienceand the Mechanistic-Computational Model of Explanation'.
- Haugeland, J. (1981) 'Semantic Engines: an Introduction to Mind Design', in
- Haugeland, J. (ed.) *Mind Design, philosophy, Psychology, Artificial Intelligence*. MIT
 Press.
- Hollerman, J. R. and Schultz, W. (1998) 'Dopamine neurons report an error in the
 temporal prediction of reward during learning', *Nature neuroscience*, 1, pp. 304–9.
 doi: 10.1038/1124.
- Hoshi, E. *et al.* (2005) 'The cerebellum communicates with the basal ganglia', *Nature Neuroscience*, 8, pp. 1491–1493. doi: 10.1038/nn1544.
- Huneman, P. (2010) 'Topological explanations and robustness in biological sciences', *Synthese*, 177, pp. 213–245.

- 692 Ito, M. and Doya, K. (2009) 'Validation of Decision-Making Models and Analysis of
- Decision Variables in the rat basal ganglia', *The Journal of Neuroscience*, 29(31), pp.
- 694 9861–9874. doi: 10.1523/JNEUROSCI.6157-08.2009.
- Ito, M. and Doya, K. (2011) 'Multiple representations and algorithms for
- reinforcement learning in the cortico-basal ganglia circuit', *Current Opinion in Neurobiology*, 21, pp. 368–373. doi: 10.1016/j.conb.2011.04.001.
- 698 Kable, J. W. and Glimcher, P. W. (2009) 'The Neurobiology of Decision: Consensus
- and Controversy', Neuron. Elsevier Inc., 63(6), pp. 733–745. doi:
- 700 10.1016/j.neuron.2009.09.003.
- Kandel, E. R. *et al.* (2013) *Principles of Neural Science*. Fifth. New York: McGraw-Hill.
- Kaplan, D. M. (2011) 'Explanation and description in computational neuroscience',
 Synthese, 183, pp. 339–373.
- Kaplan, D. M. (2017) 'Neural computation, multiple realizability, and the prospects
 for mechanistic explanation', in Kaplan, D. M. (ed.) *Explanation and Integration in Mind and Brain Science*. Oxford University Press, pp. 164–189.
- Kaplan, D. M. and Craver, C. F. (2011) 'The Explanatory Force of Dynamical and
 Mathematical Models in Neuroscience : A Mechanistic Perspective', *Philosophy of Science*, 78, pp. 601–627.
- 710 Lange, M. (2013) 'What Makes a Scientific Explanation Distinctively Mathematical?',
- 711 *The British Journal for the Philosophy of Science*, 64, pp. 485–511. doi:
- 712 10.1093/bjps/axs012.
- Lee, E. *et al.* (2015) 'Injection of a Dopamine Type 2 Receptor Antagonist into the
- 714 Dorsal Striatum Disrupts Choices Driven by Previous Outcomes, But Not Perceptual

715 Inference', *The Journal of Neuroscience*, 35, pp. 6298–6306. doi:

- 716 10.1523/JNEUROSCI.4561-14.2015.
- Li, J. and Daw, N. D. (2011) 'Signals in Human Striatum Are Appropriate for Policy
- 718 Update Rather than Value Prediction', *Journal of Neuroscience*, 31, pp. 5504–5511.
 719 doi: 10.1523/JNEUROSCI.6316-10.2011.
- Marr, D. (1982) Vision: A Computational Investigation into the Human
 Representation and Processing of Visual Information. MIT Press.
- 722 Milkowski, M. (2013) *Explaining the Computational Mind*. MIT Press.
- 723 Mnih, V. *et al.* (2016) 'Human-level control through deep reinforcement learning',
- 724 *Nature*, 518, pp. 529–533. doi: 10.1038/nature14236.
- 725 Mongillo, G., Shteingart, H. and Loewenstein, Y. (2014) 'The misbehavior of
- reinforcement learning', *Proceedings of the IEEE*, 102, pp. 528–541. doi:
- 727 10.1109/JPROC.2014.2307022.
- 728 O'Doherty, J. P. et al. (2004) 'Dissociable Role of Ventral and Dorsal Striatum in
- 729 Instrumental Conditioning', *Science*, 304, pp. 452–454. doi:

- 730 10.1126/science.1094285.
- Piccinini, G. (2015) *Physical Computation: A Mechanistic Account*. Oxford University
 Press.
- Piccinini, G. and Bahar, S. (2013) 'Neural Computation and the Computational Theory
 of Cognition', *Cognitive Science*, 34, pp. 453–488.
- Piccinini, G. and Craver, C. F. (2011) 'Integrating psychology and neuroscience:
- functional analyses as mechanism sketches', *Synthese*, 183, pp. 283–311.
- Rathkopf, C. (2015) 'Network representation and complex systems', *Synthese*, 195,
 pp. 55–78.
- Rusanen, A. and Lappi, O. (2016) 'On computational explanations', *Synthese*, 193, pp.
 3931–3949.
- Samejima, K. *et al.* (2005) 'Representation of Action-Specific Reward Values in the
 Striatum', *Science*, 310, pp. 1337–1340. doi: 10.1126/science.1115270.
- Schultz, W., Dayan, P. and Montague, P. R. (1997) 'A Neural Substrate of Prediction
 and Reward', *Science*, 275, pp. 1593–1599. doi: 10.1126/science.275.5306.1593.
- Shagrir, O. (2006) 'Why we view the brain as a computer', *Synthese*, 153, pp. 393–
 416.
- Shagrir, O. (2016) 'Advertisement for the Philosophy of the Computational Sciences',
 in Paul Humphreys (ed.) *The Oxford Handbook of Philosophy of Science*. Oxford
 University Press, pp. 15–42.
- Shagrir, O. and Bechtel, W. (2017) 'Marr's Computational Level and Delineating
 Phenomena', in Kaplan, D. M. (ed.) *Explanation and Integration in Mind and Brain Science*. Oxford University Press, pp. 190–214.
- Shapiro, L. A. (2017) 'Mechanism or Bust? Explanation in Psychology', *The British Journal for the Philosophy of Science*, 68, pp. 1037–1059.
- 755 Shteingart, H. and Loewenstein, Y. (2014) 'Reinforcement learning and human
- behavior', *Current Opinion in Neurobiology*, 25, pp. 93–98. doi:
- 757 10.1016/j.conb.2013.12.004.
- Shteingart, H., Neiman, T. and Loewenstein, Y. (2013) 'The role of first impression in
 operant learning', *Journal of Experimental Psychology: General*, 142, pp. 476–488.
 doi: 10.1037/a0029550.
- Sprevak, M. (2010) 'Computation, individuation, and the received view on
 representation', *Studies in History and Philosophy of Science Part A*, 41, pp. 260–270.
- Stich, S. (1983) From Folk Psychology to Cognitive Science: The Case Against Belief.MIT Press.
- 765 Sutton, R. S. and Barto, A. G. (1998) *Reinforcement Learning: An Introduction*. MIT

- 766 Press.
- 767 Tai, L.-H. *et al.* (2012) 'Transient stimulation of distinct subpopulations of striatal
- neurons mimics changes in action value', *Nature neuroscience*, 15, pp. 1281–9. doi:
 10.1038/nn.3188.
- 770 Wang, A. Y., Miura, K. and Uchida, N. (2013) 'The dorsomedial striatum encodes net
- expected return, critical for energizing performance vigor.', *Nature neuroscience*, 16,
 pp. 639–47. doi: 10.1038/nn.3377.
- Watkins, C. J. C. H. and Dayan, P. (1992) 'Q-Learning', *Machine Learning*, 8, pp. 279–
 292.
- 775 Weiskopf, D. A. (2011) 'Models and mechanisms in psychological explanation',
- 776 *Synthese*, 183, pp. 313–338.

777