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Article **Probability of self-location in the framework of the many-worlds interpretation**

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Abstract: The growing interest in the concept of probability of self-location of a conscious agent created multiple controversies. Considering David Albert's setup in which he described his worries about consistency of the concept, I identify the sources of these controversies and argue that defining "self" in an operational way provides a satisfactory meaning for the probability of self-location of an agent in a quantum world. It keeps the nontrivial feature of having subjective ignorance of self-location without ignorance about the state of the universe. It also allows defining the Born rule in the many-worlds interpretation of quantum mechanics and proving it from some natural assumptions.

1. Introduction

I am very pleased to contribute to this book celebrating 100 years of Born's rule. I am an academic great-great-grandchild of Max Born. My Ph.D. advisor Yakir Aharonov got his doctorate under David Bohm who was the student of Robert Oppenheimer, the student of Max Born.

I do not know what role Born's rule played in the research of Robert Oppenheimer, 14 although it is clear that it is needed for calculating the probability of nuclear chain reaction. 15 David Bohm [1] took the Born rule as a postulate in his theory of hidden variables. It 16 allowed him to remove randomness from dynamical evolution by putting it into the initial 17 distribution of Bohmian particle positions in the universe. Yakir Aharonov also adopted the 18 Born rule (less explicitly) with another proposal to avoid dynamical randomness [2]. He 19 postulated backward evolving quantum state which corresponds to the outcomes of future 20 measurements which exhibit Born rule statistics. Aharonov, Bergmann, and Lebowitz [3] 21 generalized the Born rule to measurements performed on pre and postselected quantum 22 systems (in contrast to measurements on systems which are preselected only), what is 23 known as the ABL rule. The time-symmetric approach to quantum measurements created 24 significant controversy [4,5], and my first contribution was the defense of the ABL rule 25 [6,7]. Since then, the Born rule has played a central role in my research, including recent 26 analysis of the derivations of Born's rule [8]. 27

Today we accept randomness in nature and it is Born's rule that is responsible for this 28 [9]. However, I remained with the conservative view preferring deterministic theories, and 29 I consider that my most important contribution related to Born's rule is finding a way to 30 define its counterpart in a deterministic quantum theory, the many-worlds interpretation 31 (MWI) [10]. Tappenden [11] named it the Born-Vaidman rule. I introduced this concept 32 through discussion probability of self-location which recently gained an increasing interest. 33 Stanford Encyclopedia of Philosophy assigns a specific entry to self-locating beliefs [12]. 34 Very recently, several authors seriously considered speculations according to which we live 35 in computer simulations [13,14], although Adlam [15] is skeptical regarding the implications 36

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of these applications of self-locating probabilities in scientific contexts. Perhaps the biggest surprise is an enormous interest in the Elga-Lewis controversy about the Sleeping Beauty scenario, [16], [17], as well as a large attention to application of this concept to defeat Dr. Evil [18].

According to the MWI, after performing a quantum measurement, an observer splits 41 into agents in different worlds, and one may want to attach probabilities to the agent of 42 being in different worlds. The situation of self-locating in the MWI is closer to the case of 43 Dr. Evil considering the probability of being Dr. Evil on the moon or being Dup on Earth, 44 see [18], than to the case of Sleeping Beauty being uncertain about the day she is currently 45 in, see [16]. Note that there is also extensive literature on Sleeping Beauty in the quantum 46 world [11,19–26]. 47

In this paper, I will defend the concept of self-location probability in the MWI framework. I will argue that the concept of self-location is necessary for understanding the Born statistics of results of quantum experiments in the framework of the MWI. In my view, numerous controversies about this concept can be satisfactorily resolved by a precise definition based on the operational meaning of the identity of an agent. For my analysis, I will consider a teleportation scenario introduced by Albert [27]. I disagree with Albert about some (important) details, but I agree with his conclusions that self-location probability in the MWI requires a radical modification of the scientific paradigm. However, contrary to Albert, I will argue that this is the best way to solve the measurement problem of quantum mechanics.

I will start with presenting Albert's classical teleportation setup in Section 2 and the quantum setup in Section 3. In Section 4 I will argue that the MWI without ontology beyond the quantum state of the universe does not allow a popular four-dimensional worm view of an agent. In Section 5 I will modify Albert's quantum setup to provide a meaningful concept of self-location probability and will argue that although it is radically different from the standard scientific paradigm of analysis of nature in objective terms, we do not have a better alternative. After establishing the meaning of self-location probability in subjective terms, in Section 6, I turn to the question of a quantitative description of this probability. What are the assumptions, if any, to derive the Born rule? In particular, I will show how it can be derived from assuming that local unitary operation cannot affect anything in remote locations. In Section 7 I briefly summarize my optimistic view on self-location probability in the MWI.

2. Albert's setup: Classical teleportation

To set up the stage for my analysis, I will use a setup considered by Albert [27]: Captain Kirk is about to step into the transporter, to beam down to the planet below. He happens to know that the transporter is malfunctioning at the moment – to wit: the transporter is going to make two Kirks on the surface of the planet out of the one that steps in on the ship, each of them dressed in a different color – one blue, one green. Both the Kirks initially arrive on the planet with their eyes closed – and (more generally) with no indication whatever of which particular one of the two Kirks on the planet they are. But each of them knows that they have arrived on the planet, and each one says to himself, correctly, that "there is now some perfectly determinate fact of the matter about which particular one of those two Kirks I am". And each of them wonders which particular one they might be. And then they open their eyes and find out. So – consider this moment, after they have arrived on the planet but before they have opened their eyes – when each of the Kirks is wondering which particular one of the Kirks he is. Lots of people – a whole academic industry of people – seem to think it makes sense

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for these Kirks to talk to themselves about "the probability that, when I open my eyes, I will find that I am this particular Kirk or that particular Kirk", or "the probability that, when I open my eyes, I will see that I am wearing a blue outfit". And this kind of talk would seem to amount to a way out of the puzzle that I mentioned above – this would seem to offer us a way of talking intelligibly about 'the probability that I am about to have this experience' and 'the probability that I am about to have that experience' even in circumstances in which I already know absolutely everything about the future physical condition of the world. The idea is that even in circumstances in which I have no ignorance whatsoever about the future objective physical condition of the world, I might still be ignorant – just as these various Kirks are ignorant, when they are standing on the surface of the planet with their eyes closed - about where I am located in it. People call these sorts of probabilities "Self-locating" probabilities …

There is nothing quantum in this setup, but even in this situation, Albert finds discussion of probability confusing. I am interested in the quantum case, but let me first offer a simple operational analysis of this classical case to prepare the ground for the quantum setup.

Most analyses of self-location beliefs introduce "worlds" and "centered worlds" [28]. 103 Instead, I propose to focus on the identity of the agent. In this setup we have two "Kirks" 104 on the planet. They differ by their outfit: green or blue, but since we are talking about two 105 people in the framework of classical physics, they also must differ in their location on the 106 planet. Thus, we have one Kirk, say, with a green outfit on the left and another Kirk with 107 a blue outfit on the right. Tappenden [29] considered a "single-mind" Kirk, defined by 108 his sentient state (which can be considered as the relative state of particles in Kirk's brain) 109 irrespective of the location in space relative to the planet. This "Kirk" is present both on the 110 left and on the right. I will argue below that this metaphysical approach to identity of an 111 agent will not lead to an operational concept of probability. 112

The operational meaning of the subjective probability of a particular fact for an agent can be modeled as the part of the dollar that the agent is ready to pay for a game in which he gets a dollar, if the fact is true, see [30]. Since all Kirks have the same sentient state, they must have identical answers to every question. If an external agent asks one of the Kirks to bet on being the Kirk with a blue outfit, will he be ready to pay fifty cents for the game? For Albert's setup we expect probability 0.5.

Let us describe the situation with more care. An external agent comes close to one 119 of the Kirks, who is awake but did not open his eyes, and offers this game for fifty cents: 120 Should Kirk agree to play? Albert, I believe, would say that Kirk has no clue about the 121 color of his outfit and that he has to refuse. I agree that Kirk should refuse. The external 122 agent sees the color of Kirk's outfit and would not offer the game to Kirk in a blue outfit. 123 Thus, Kirk is certain to lose. However, I think that Kirk on the left and Kirk on the right 124 have a subjective probability 0.5 for the green (as well as blue) outfit. When an external 125 agent approaches, each of the Kirks is ready to pay fifty cents for a game in which they get 126 a dollar when the color of their outfit is the one *they* chose (before opening their eyes). All 127 that is required to have an expected payoff is that Kirk has the ability to choose, keeping 128 external agents ignorant about his choice. This ability will not help to define the probability 129 for a "single-mind" Kirk because there is no matter of fact about the color of his outfit. 130

3. Albert's setup: Quantum teleportation

Let us move on to the quantum case. I name it "quantum teleportation" since we have a scenario with a transporter and quantum superposition, but note that it is very different

from what is usually named quantum teleportation: the protocol that transfers a quantum ¹³⁴ state using prior entanglement and a classical channel. Albert continues: ¹³⁵

Imagine (then) that the adventures of Kirk in the transporter correspond to an actual, quantum-mechanical, Everettian splitting. Imagine (that is) a quantum-mechanical measurement – say a measurement of the x-spin of an electron that is initially in an eigenstate of z-spin - whose result is encoded in the color of Kirk's outfit. Kirk's outfit is like the pointer on the measuring-device, and the color of his outfit is the position of the pointer, and Kirk himself is the sentient observer – and he becomes aware of the outcome of the experiment when he opens his eyes. And the thought is that the quantum-mechanical probability that Kirk will see this or that particular outcome of this measurement is precisely the self-locating probability that "I, Kirk" or "I, among the Kirks", or whatever it is that I call myself, am going to find, on opening my eyes, that my outfit is this or that particular color.

In classical teleportation we had two Kirks on the planet: one on the left and one on the right. We do not have two Kirks in the quantum case. I think the option that Albert considers: "I, among the Kirks" does not exist. We consider Kirk before he opens his eyes when he is not aware of the outcome. My reading of Albert is that whatever Kirk is, at this stage, there is no entanglement between Kirk and his outfit, so there are no two different states of the captain. There is a single Kirk with an outfit in a superposition of being blue and green.

One may be concerned about the issue of decoherence: How can the outfit be in a superposition of macroscopically distinguishable states (green and blue), while Kirk, wearing it, is in a pure state not entangled with the states of the outfit? A model in which the outfits with different colors cause difference in the Kirk's brain only after he opens his eyes seems possible (surely possible if teleportation of Kirks is possible), and this is the scenario considered here.

Note that even if we consider a scenario in which decoherence will lead to a macro-161 scopic number of molecules in Kirk's brain to be strongly entangled with the color of the 162 outfit, I still would prefer not to consider two Kirk's here. "Kirk" is a quantum state of 163 particles which specifies a three-dimensional pattern in a shape of the captain, see [31]. 164 The superposition of such states in remote locations corresponds to multiple Kirks. The 165 superposition of states in the same macroscopic location, but describing brains in different 166 knowledge states of the color of the outfit also corresponds to different Kirks. However, 167 in the situation described in Albert's setup, I see only one Kirk. He knows the situation: 168 the outfit might be entangled with parts of his brain, but not the parts of the brain that 169 supervene on his awareness now. Thus, for Kirk with awareness, there is no matter of fact 170 about the definite color of the outfit. Kirk knows that the outfit and parts of his brain are 171 in mixed states. In the semantics of [32], Kirk is still in the state of "abscent self-location 172 uncertainty". There are no two Kirk's because there are no two different macroscopic 173 bodies corresponding to two different sentient states. Given decoherence, there are two 174 different autonomous branches which do not exhibit interference, but there is no "Kirk" 175 who is uncertain in which branch he is. 176

Albert is not the only one who takes this (in my view, illegitimate) approach. Tittelbaum [33] writes in Section 10:

... For instance, take the time immediately after the [Stern-Gerlach] experiment has been run but before anyone has observed its outcome. At that time, there are two agents in two universes. Each of those agents is about to measure a different outcome, ...

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I deny the possibility of talking about two agents at this stage.

More recently, Wilson [34] writes:

... subsequent to a Stern-Gerlach measurement I can know that there is an x-spinup world and a x-spin-down world but not know which of these two worlds I am in. These self-locating contents are no mere curiosity: for many Everettians they provide the subject-matter for objective probabilities in EQM [35–39].

I argue that in Wilson's setup I am in both worlds together, so I cannot ask myself in which 189 world am I. In the literature mentioned by Wilson there are formal semantic definitions 190 for this question, but I argue that the consideration of this question is improper. For 191 example, the derivation of the Born rule by Sebens and Caroll [39] fails if the question lacks 192 operational meaning for alternatives, see [32,40], and other discussions of the Sebens-Caroll 193 proof [41,42]. 194

The operational meaning discussed here is the possibility (even if it is a gedanken with 195 today's technology) using physical (local) interactions to observe the difference between 196 the agents (Kirks) before they open their eyes (i.e. during short period of time and not 197 by viewing agent's history). The "agent" is considered as a minimal part of the brain 198 containing the information about its sentient state. The "brain" is modeled as wave 199 function of relative spatial coordinates of its constituents together with the brain's position 200 relative to a macroscopic frame of reference. The absolute position should be considered 201 since macroscopic objects (agents) cannot, by definition, be in a superposition of different 202 locations even if they have identical relative states (contrary to the single-mind agent of 203 Tappenden [29]). Agents in different locations can easily be distinguished in an experiment 204 that provides operational meaning for probability in the sleeping pill experiment [43], in 205 which a superposition of identical relative coordinate spatial wave functions of the agent 206 particles is created that differ macroscopically by their position in space. 207

Note that although for various analyses it is crucial that in the moment we try to define 208 the probability of self-location there is a matter of fact about belonging to a particular world, 209 an agent may nonetheless have other reasons for placing bets on different outcomes. He 210 can do this because he cares more for some of his descendants than others, being aware 211 that all of them will exist, see [43,44]. 212

4. Against spacetime worms view of agents

Even among proponents of the MWI, the majority is reluctant to accept that we cannot 214 ask a simple question: What is the probability of an outcome of a quantum measurement? 215 It seems that at least after the measurement, when the worlds with different outcomes are 216 created, the question is legitimate. It is very natural that in different worlds live different 217 agents, so apparently we can ask: In what world do I (the agent) live? This question also fits 218 well with the view of "spacetime worms" [45], according to which an agent is defined as a 219 four-dimensional worm in spacetime. There is a matter of fact about the world in which a 220 particular four-dimensional worm appears. However, I argue that this approach fails. The 221 ontological counterpart of an agent in the MWI is the wave function of the particles from 222 which he is composed. Until the agent becomes entangled with the result of the quantum 223 measurement, there is only one entity like this. In a deterministic theory such as MWI, the 224 entity will evolve into a single particular "thing". This "thing" can be a set of agents, but 225 we cannot have an uncertainty about what the entity will become. 226

The lack of operational meaning has not prevented authors from making semantic 227 statements considering two Kirks. Saunders [46], then Wallace [47], then Lewis [48] argue 228 that we can consider two Kirks before the measurement, as can be seen in the quote from 229 Lewis [48]: 230

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We can, if we wish, adopt the Lewis criterion for personal identity in Everettian contexts, in which case there are (in that sense) two persons prior to measurement. We could even give these two persons names, say she^{\uparrow} and she^{\downarrow}, so that she^{\uparrow} refers to the person who sees 'up' and she^{\downarrow} refers to the person who sees 'down'. If I walk into the lab and ask "What result is she about to see?", I might be told "she^{\uparrow} will see 'up' and she^{\downarrow} will see 'down', and at the moment she^{\uparrow} and she^{\downarrow} coincide".

Saunders and Wallace [35] even claim that we can adopt Lewis's approach that there are two persons present before branching not only for divergent worlds, but also for branching worlds:

... it is now rather clear, from Section 2, what we are ignorant: we don't know which world - which branch, big-bang to end-of-time – is ours. It is lack of knowledge *de se*, uncertainty of where we located, not as a stage *S* but as a worldstage $\langle W, S \rangle$ or world-time $\langle W, t \rangle$, among the branching worlds. Ignorance on this score makes rather obvious sense in case of diverging worlds, and now we are in a position to see that it makes just much sense, on our semantics, in the case of branching worlds.

I find that these formal metaphysical attempts lead only to difficulties. The standard physics paradigm relies on agents described locally in spacetime points. The MWI branch-249 ing structure does not support the diachronic identity of a person toward the future. If she^{\uparrow} and she^{\downarrow} coincide, they cannot lead to different "she"s later. When she^{\uparrow} and she^{\downarrow} 251 "coincide" there is nothing to distinguish them. Thus, if we do want to consider "she" 252 as a spacetime worm, we must have a picture of "splitting worms". "She" before the 253 measurement splits into she^{\uparrow} and she^{\downarrow}. This picture still provides a unique description of 254 "she" in the past. Before the measurement, the identity of she^{\uparrow} who sees 'up' is "she prior 255 to measurement". This is also the identity before the measurement of she^{\downarrow} who sees 'down' 256 after the measurement. In contrast, the future of a "she" is not another "she", but rather a 257 set of "she"s. 258

The proponents of the worm view often bring the analogy with roads with different 259 names, which have nevertheless a partial overlap. A driver, moving in the common part, 260 may ask herself a question about the road she will choose when the roads separate. She 261 might know this before splitting or may decide when she arrives at the fork. However, if 262 she is like a photon reaching a beamsplitter that splits and goes in both ways, then there is 263 no matter of fact before the spitting which path she will take. The worm view with past 264 and future has a perfect sense if we add some ontological entity, like a Bohmian position 265 in configuration space of agent's particles, see [1], or an ontic "mind" of an agent in the 266 Albert-Loewer approach [49]. I see no room for a future evolving worm when the only 267 ontology is the quantum state of the universe. Returning to the analogy with overlapping 268 roads, at the place of the overlap, we do have additional ontological entity: the name of the 269 road. 270

5. Modified quantum teleportation and Albert's conclusions

There is no consensus among proponents of the MWI regarding what is a world in the MWI, so it is not surprising that worlds might lead to confusion in understanding self-location of an agent. Undoubtedly, the concept of a centered world is fruitful in many situations, but it has some ambiguities, see [50]. I argue that we can discuss the self-location centering the agent directly.

Due to the locality of physical interactions, we have operational meaning for selflocation of an agent in space. An agent can see what is around him and, comparing with a map, know where he is. So, a modification of Albert's quantum setup which allows the

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objective knowledge. Toward the end of his lecture [27], Albert reaches the conclusion that the claims about probabilities of self-location are "irreducibly indexical". He argues that

classical cases have the peculiar property of subjective uncertainty in a state of complete

we should not say, and the science of such probabilities should not aspire to say, that this or that theory of the assignment of self-locating probabilities is well confirmed by experiment, or that there are good reasons to believe it, or that it is true or false of the world. What we should say, and all that the science of such probabilities should aspire to say, is that the theory in question is well confirmed for *me* by experiment, and that there are good reasons for *me* to believe it, and that it is true or false of the world that is centered on myself ...

Albert considers this conclusion outrages:

... the important thing to say is that, if probabilities like these are supposed to play a central role in scientific explanations, if probabilities like these are supposed to play the role for example of quantum mechanical chances, then this way of thinking is going to radically diminish the traditional objective realistic aspirations of the scientific project, and the question is why in the world we would even want to fool around with crazy sh*t like this, when there are sensible and workable and flat-footedly mechanical ways of solving the measurement problem on the table ...

Yes, the probability of self-location is intrinsically subjective. There is no way for an 307 external agent, a super-technology which can manipulate and measure superposition of 308 Kirks wearing different outfits, to confirm or disconfirm Kirk's subjective self-location 309 probabilities. However, the agent's subjective probabilities in the modified Albert's telepor-310 tation to different locations are objective properties of our universe. They are confirmed by 311 my subjective evidence as an agent performing quantum experiments. Formally, Albert is 312 correct: In a single world of quantum mechanics with collapse, my empirical evidence is 313 the only one that exists, so it can be named objective instead of subjective. However, since 314 the experience of agents in every Everett world is identical to the experience of an agent 315 in the single world with corresponding collapses, I fail to see a difference in an empirical 316 evidence of the agents in the two cases. The standard objection about the definite existence 317 of maverick worlds in MWI in contrast with only low probability of existence of a maverick 318 world in the universe with collapses seems to me a manifestation of the known difficulty of 319 the frequentist approach to probability without infinite ensembles. 320

I agree that this is a radical change of the traditional way of thinking that a law of 321 evolution of ontic entities (the law of evolution of the quantum state of our universe) is 322 not the full description of nature and we have to complement it by a postulate about 323 subjective self-location probabilities of sentient agents (the counterpart of the Born rule 324 in MWI). However, I think that this radical change is forced upon us by the many-worlds 325 picture. The quantum theory without collapse also forces us to accept the existence of 326 a macroscopic superposition corresponding to a dead and alive cat, which is viewed as 327 absurd by Schrödinger. And the reason to take MWI seriously is because alternative 328

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solutions of the measurement problem have arguably worse features: action at a distance 329 and randomness, see [51].

6. Quantitative analysis: the Born rule

I introduced two modifications of Albert's setups: (1) the agent decides what is the 332 winning option of the bet, and (2) in the quantum case, the position of the agent himself 333 is changed according to the result of the Stern-Gerlach experiment. These changes allow 334 for a legitimate concept of subjective probability in an operational way. It might well be 335 that Albert accepts (1) implicitly. (2) seems to be crucial: without it, Kirk cannot ask the 336 question of self-location. 337

Now we can turn to the quantitative analysis. What is the numerical value of probabil-338 ity for a particular self-location? We have vast empirical data showing that the probability 339 follows the Born rule, but we also have a very extensive literature suggesting that this 340 result can be derived from unitary quantum mechanics alone, e.g. [39,52,53]. I believe 341 that the Born rule cannot be proven without some additional assumptions [8], and that 342 the current proofs either take some implicit assumptions, or use incorrect argumentation 343 based on manipulation of meaningless concepts like probability of self-location of Kirk in 344 unmodified Albert's quantum case. 345

It is straightforward to show, based on world counting, that the case of agents belong-346 ing to equal-amplitude worlds corresponds to the Born rule probability. Saunders [54], 347 using the decoherent histories formalism, argues that agents can always be represented in 348 this way, providing a new route to probability. He continued this approach [55], but ques-349 tioned the role of decoherence: "Does quantum probability always involve decoherence?" 350 Following ideas of Boltzmann and Gibbs, Saunders suggested finite quantum frequentism 351 [56] by counting the number of equal-amplitude parts of the wave function corresponding 352 to a particular outcome and dividing it by the total number of such equal-amplitude parts 353 in the wave function. Although this approach provides a nice description of the Born 354 Rule, I do not see in which sense it might be considered as its derivation. It is based on 355 the analogy with classical statistical theory, but there is a difference: in the classical case, 356 always there is a matter of fact (maybe unknown to us) about the state of a system, while in 357 the quantum case (without hidden variables) there is no matter of fact about the part of the 358 quantum wave to which the system belongs, so there is no place for uncertainty. 359

Another difficulty of Saunders's approach appears in the analysis of a Stern-Gerlach 360 experiment with a spin in the initial state very close to one of the measured spin-component 361 eigenstates, say "up". The physics of the detector showing "up" is very much the same 362 as the physics of the detector showing "down", but since the probability of "up" is much 363 larger, we must have many more orthogonal parts of the wave function of equal amplitude 364 for "up" than for "down". Thus, the parts corresponding to "up" must have a very different 365 shape than those corresponding to "down". This represents tension with the principle of 366 counting all equal-amplitude parts equally. See another analysis of Saunders's proposal by 367 Khawaja [57]. 368

One can also find authors, e.g. Putnam [58], who treat all agents with non-vanishing 369 amplitude states on equal footing, even if the amplitudes of the corresponding states are 370 different. In this way, the derived probability rule within MWI contradicts empirical data 371 and leads them to dismiss the MWI. The basis for these derivations is the "naive principle 372 of indifference", see [59] according to which all options compatible with the evidence of 373 the agent should be assigned equal probability. The rational for applying the principle of 374 indifference for self-location beliefs is that, by construction, the agents in all cases have the 375 same sentient state. Moreover, since the agents are placed in separate locations, different 376 unitary operations can be applied in these locations, ending up in a situation in which 377 all agents and their nearby environments will have identical quantum states. (Locality 378 suggests that each local unitary operation cannot change the probability of self-locations. 379 Although in general, locality does not prevent changes in the location of the local operation, 380 the probability of self-location cannot be changed locally because the total probability is 381 1 and a local change of the probability invariably changes some probabilities in remote 382 locations which locality does not allow.) Thus, we reach a situation in which local agents 383 not only have the same sentient state, but also have no means of distinguishing between 384 different locations by investigating their surroundings, in contrast to Dr. Evil and the 385 brain in a vat discussed in [18]. This type of analysis apparently led Putnam to apply the 386 indifference principle in this case. 387

However, I argue that this is a mistake. Subjective indistinguishably is not enough. The indifference principle requires that we have no reasons to prefer one location over the other. This is not the case here. We can arrange identical quantum states by local actions in all parameters except for one, the absolute value of the amplitude of the terms in the superposition corresponding to agents in various locations. If the amplitudes are different, then the agents are different, so we cannot claim that "there are no reasons to prefer one over the other".

A very natural assumption that has roots in the "additivity requirement" of Everett 395 [10] is that the local splitting of an agent into a number of agents in close-by locations should 396 lead to the sum of the probabilities to be found in all of them equal to the probability to be 397 found in this place before the splitting. (It is similar to Weak connection with transformations, 398 the third "reasonable" axiom of Short [60].). This property follows from locality in a similar 399 way as discussed above regarding the independence of self-location probability of an agent 400 undergoing local unitary evolution. Locality prevents immediate changes of the probability 401 of self-location in a bounded region. By introducing more splittings, see [52], we can 402 arrange equal amplitudes for all agents. I [61], suggested adding local operations that make 403 all local states that describe agents identical. Arranging these states in a geometrically 404 symmetrical configuration leads to really identical agents, so there will be no way to prefer 405 one over the other. In this scenario, the principle of indifference can be applied to derive 406 an equal self-location probability of split agents of equal amplitude. This construction, 407 together with the standard quantum formalism, leads to the Born rule for the general case 408 of unequal-amplitude agents. Zurek [62], makes another assumption to derive the Born 409 rule. He assumes a natural "envariance" feature of entangled systems. Wallace [63] puts 410 Deutsch [52] ideas on more rigorous grounds by evoking postulates of decision theory. I 411 find that Wallace's postulates include some assumptions that go beyond unitary quantum 412 mechanics. 413

All interpretations of quantum mechanics have the Born rule as an additional postulate. 414 (I am skeptical about Valentini's attempt to derive the Born rule in the framework of 415 Bohmian mechanics, [64].) In the MWI, the situation is worse: even defining the postulate 416 of the Born rule is difficult because it does not correspond to any objective statement about 417 the ontic state of the universe. The concept of self-location probability in special situations 418 of an agent who is uncertain about the world in which he is (when there is a matter of 419 fact about it) allows us to define ignorance probability in a familiar betting setting. The 420 postulate that the agent, ignorant of the world in which he is in, has to bet according to the 421 "measure of existence" of this world, see [51], explains Born rule statistics for experiments 422 performed in such a way; that is, experiments with a stage in which the results are obtained, 423 macroscopically different agents are created, but they are still ignorant about the outcome. 424 Most experiments are not like this, so the postulate of betting according to the measure of 425 existence does not lead to the formal derivation of the Born rule in these cases. However, 426 it does not sound plausible that blindfolding or not blindfolding of the observers before 427

Maybe a simplest way to make a postulate is to declare that we should expect to be 432 located in the world with the Born rule statistics of the results of quantum experiments. 433 Clearly, this postulate does not provide a very informative explanation of the Born rule, 434 but I find it meaningful. It is a statement about our subjective information in a particular 435 world, but it describes the law of nature (which does not follow from the unitary dynamics 436 of quantum theory) relevant to the whole universe of the MWI. This move does not nullify 437 the value of numerous derivations of the Born rule based on various natural assumptions, 438 because they show plausibility of the postulate. 439

7. Conclusions

The concept of self-location probability leads to debates that span from speculation that we live in a computer simulation, to arguments that the MWI is inconsistent, and to a controversy about the proof of the Born rule. Adlam [15] just published a paper "Against self-location", while Chen [65] writes: 444

As the case study shows, postulating self-locating probability in physics is like opening a Pandora's box: it is full of conceptual difficulties. We may wonder whether it is appropriate to allow self-locating postulates in physics

I believe that these difficulties appear when we use an abstract approach to science consid-448 ering a wide range of metaphysical options. I argue that if we limit ourselves to standard 449 practice in physics grounded in operational meaning, this concept is useful and even nec-450 essary. The confusion, controversy, and paradox of the probability of self-location follow 451 from the formal concept of "self". Considering "self" as an entity which is local in space, 452 local in time, and which is macroscopically different from any other self (possibly only due 453 to location in space) allows a satisfactory concept of probability of self-location which keeps 454 the nontrivial feature of having subjective ignorance of self-location without ignorance 455 about the state of the universe. 456

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