The End of the Thermodynamics of Computation: A No Go Result

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The thermodynamics of computation assumes that computational processes at the molecular level can be brought arbitrarily close to thermodynamical reversibility; and that thermodynamic entropy creation is unavoidable only in data erasure or the merging of computational paths, in accord with Landauer's principle. The no go result shows that fluctuations preclude completion of thermodynamically reversible processes. Completion can be achieved only by irreversible processes that create thermodynamic entropy in excess of the Landauer limit.

1. Introduction

Electronic computers degrade work to heat and the need for its removal sets a practical limit to their performance. The study of the thermodynamics of computation, surveyed in Bennett (1982), seeks the limits in principle to reduction of this dissipation. Since dissipation reduces with size, the most thermodynamically efficient computers are sought among those that use individual molecules, charges or magnetic dipoles as memory storage devices.

These molecular-scale processes are treated like macroscopic ones in one aspect: they can be brought arbitrarily close to the most efficient, non-dissipative processes, those that are thermodynamically reversible. Their defining characteristic is that they are at equilibrium at every stage. They are brought slowly from start to finish by the successive nudges of miniscule disequilibria. It is assumed that the dissipative effects of these nudges can be made arbitrarily small by indefinitely extending the time allowed for the process to reach completion.

Some form of dissipation, however, is judged unavoidable. The controlling idea of the thermodynamics of computation is that the creation of thermodynamic entropy and the associated need to pass heat to the environment arise only with logically irreversible operations. These include the erasure of data and the merging of computational paths. The amount of thermodynamic entropy created is quantified by Landauer's principle. It asserts that at least k ln 2 of thermodynamic entropy is created when one bit of data is erased. The result is an elegant account of the bounds to the thermodynamic efficiency of computation. They are independent of the physical implementation, but are set by the logical operations comprising the computation.

Alas, this image of a well-developed science is an illusion. The thermodynamics of computation is an underdeveloped muddle of vague plausibility arguments and misapplications of statistical physics. Earman and Norton (1998, 1999) track the science's history through the Maxwell demon problem and find it rife with circular reasoning and question begging. Norton (2005, 2011) urges that the arguments used to support Landauer's principle are fallacious and have never successfully advanced beyond flawed plausibility arguments. Erasure may reduce the range of possible values for data in a memory. But this reduction is not a compression of the accessible phase space of thermodynamic components that can be associated with a change of thermodynamic entropy. The volume of accessible phase space remains unchanged in erasure. Prior to erasure we may also be unsure as to the data stored and assign probabilities to the possibilities. That sort of probability, however, is not associated with a thermodynamic entropy.

Finally, Norton (2011) describes a "no go" result—that thermodynamically reversible processes at molecular scales are precluded from proceeding to completion by fluctuations. Individual computational steps can only be completed if they are sufficiently far from equilibrium to overcome fluctuations. As a result they create quantities of thermodynamic entropy in excess of those tracked by Landauer's principle. It follows that the lower limit to thermodynamic entropy creation is not set by the logical specification of the computation, but by the details of the particular physical implementation and the number of discrete steps it employs, whatever their function.

This paper will develop the no go result. It is motivated and then stated in the next section. In Section 3, it is illustrated; and in Section 4 a possible loophole is described and closed.

2. The No Go Result

2.1 A Preliminary Form

In a thermodynamically reversible process,¹ all component systems are in perfect equilibrium with one another at all stages. As result, they are impossible processes.² Nothing changes. Heat will not spontaneously pass from one body to another if they are at the same temperature. In ordinary thermodynamics, this awkwardness is overcome by introducing a slight disequilibrium. We minutely raise the temperature of the first body and let that minute temperature gradient drive the heat transfer, slowly. Because heat is now passing spontaneously from hot to cold, this is a dissipative process. The thermodynamic entropy created measures the amount of dissipation. For theoretical analyses, this entropy creation can be neglected since it can be made as small as we like by making the driving temperature difference appropriately small. The process will still go forward, but more slowly.

Matters are different when we allow for the molecular constitution of matter. For now the equilibrium of a thermodynamically reversible process is dynamic. If two bodies at the same temperature are in thermal contact, energy will spontaneously pass to and fro between them as energy fluctuations due to random, molecular-scale events. If we are to assure that heat passes

¹ Typical erasure processes begin with a thermodynamically irreversible process in which the memory device is thermalized. For example, the wall dividing a two-chamber memory cell is raised so the molecule can access both chambers. The resulting uncontrolled, thermodynamically irreversible expansion creates the k ln 2 of thermodynamic entropy tracked by Landauer's principle. As Norton (2005, Section 3.2) argues, a mistaken tradition misidentifies this thermalization as thermodynamically reversible since the replacing of the partition supposedly returns the original state of "random data."

² For an analysis of thermodynamically reversible processes, see Norton (forthcoming, §3).

from the one to the other, we must arrange for a disequilibrium that is sufficiently great to overcome the fluctuations.

Boltzmann's Principle, " $S = k \ln W$," that is, "entropy = $k \ln P$ probability," measures the dissipation needed. An isolated system is to pass from state 1 with total thermodynamic entropy S_1 to state 2 with total entropy S_2 . The inverted principle tells us that, if the system can spontaneously move between the two states, then the probabilities P_1 and P_2 of the two states are related by

$$P_2/P_1 = \exp((S_2 - S_1)/k) \tag{1}$$

In macroscopic terms, negligible thermodynamic entropy creation is sufficient to drive processes to completion. If S_2 - S_1 = 10k, a macroscopically negligible amount, we find P_2/P_1 = 22,026, so that the final state 2 is strongly favored.

At the molecular level, these amounts of thermodynamic entropy are large. They exceed the entropy change of k $\ln 2 = 0.69$ k tracked by Landauer's principle. They must exceed it, for creation of merely k $\ln 2$ of entropy is insufficient to assure completion of a process. Then $P_2/P_1 = \exp (k \ln 2/2) = 2$. The process is only twice as likely to be in its final state 2 as in its initial state 1. This is a fatal result for the thermodynamics of computation. If we have any computing process with multiple steps operating at molecular scales, we must create thermodynamic entropy in each step if the process is to go forward, quite aside from any issues of logical irreversibility.

2.2 The Main Result

Boltzmann's Principle in the form (1) applies to isolated systems. In the thermodynamics of computation, the computing systems are treated as open systems, in equilibrium with a heat bath at the ambient temperature T. The main result arises when we adapt these considerations to such systems.

A computer is a system consisting of many interacting components, including memory cells, systems that read and write to the memory cells and other control components to implement the computer's program. At any moment, the combined system is in thermal equilibrium with the environment at temperature T. Hence, the system is canonically distributed over its phase space, according to the probability density

$$p(\mathbf{x}, \boldsymbol{\pi}) = \exp(-E(\mathbf{x}, \boldsymbol{\pi})/kT)/Z$$

where Z is the normalizing partition function and \mathbf{x} and $\boldsymbol{\pi}$ are multi-component generalized configuration and momentum coordinates.

Each computational step is carried out by a thermodynamically reversible process, whose stages are parameterized by λ . Fluctuations will carry the system spontaneously from one stage to another. As a result, the system is probabilistically distributed over the different stages. The probabilities are computed by Einstein's methods, as adapted by Tolman (1938, pp. 637-38), and conform to the probability density

$$p(\lambda) = \text{constant. } Z(\lambda)$$
 (2)

where $Z(\lambda)$ is given by

$$Z(\lambda) = \int_{\lambda} \exp(-E(\mathbf{x}, \boldsymbol{\pi})/kT) d\mathbf{x} d\boldsymbol{\pi}$$

This last integral extends over the volume of phase space accessible to the system when the process is at stage λ .

In the Einstein-Tolman analysis, each of these stages is given a thermodynamic description as if it were an equilibrium state, even though it may have arisen through a fluctuation. The canonically distributed system at stage λ is assigned a canonical free energy

$$F(\lambda) = -kT \ln Z(\lambda) \tag{3}$$

treating $Z(\lambda)$ as a partitition function, where the free energy is defined as

$$F(\lambda) = E(\lambda) - TS(\lambda)$$

Here $E(\lambda)$ and $S(\lambda)$ are the mean energy and the thermodynamic entropy assigned to the system in stage λ . It now follows from (2) and (3) that

$$p(\lambda) = constant. exp(-F(\lambda)/kT)$$

and that the probability densities for the system fluctuating between stages λ_1 and λ_2 satisfy

$$p(\lambda_2)/p(\lambda_1) = \exp(-(F(\lambda_2) - F(\lambda_1))/kT)$$
(4)

The process is thermodynamically reversible. Hence it is in equilibrium at every stage. Equilibrium requires the vanishing of the generalized thermodynamic force $X(\lambda)$ acting on the system:³

$$X(\lambda) = -\partial/\partial \lambda|_T F(\lambda) = 0$$

Integrating over λ , we find that the free energy $F(\lambda)$ is constant over the stages of the process:

$$F(\lambda) = constant$$
 $F(\lambda_1) = F(\lambda_2)$ (5)

From (4), we have that

$$p(\lambda) = constant$$
 $p(\lambda_1) = p(\lambda_2)$ (6)

This last result (6) is the no go result. It precludes thermodynamically reversible processes proceeding as we expect.

Our default expectation is that these processes are in a quiescent equilibrium at every stage λ , perhaps with a slight disturbance due to fluctuations. We expect to bring the process from its initial to its final stage by minute disequilibrium nudges that advance the process arbitrarily slowly in the tiniest of steps. What (6) tells us is that fluctuations obliterate the quiescent equilibrium. If the system is in one stage λ at some moment, it is equally likely to be found at the next moment at any other stage. If we set up the process in its initial stage, it is as likely to leap by a fluctuation to the final stage as it is to stay where it is. If the process has arrived at the final stage, it is as likely to be flung by a fluctuation back to its initial stage, as it is to stay where it is. In a slogan, fluctuations obliterate thermodynamically reversible processes.

Fluctuations are temperature sensitive. Hence we might expect the confounding effects of fluctuations to be calmed and controlled by cooling the processes, perhaps even close to absolute

 $^{^3}$ At equilibrium, the total entropy S_{tot} of the system S_{sys} and the environment S_{env} is stationary. Writing $d=\partial/\partial\lambda|_T$, that amounts to $0=dS_{tot}=dS_{sys}+dS_{env}.$ By supposition, the computer system exchanges no work with the environment, but only heat in a thermodynamically reversible process. Hence $dS_{env}=dE_{env}/T=-dE_{sys}/T,$ where the last equality follows from conservation of energy: $dE_{env}+dE_{sys}=0$. Combining, we have $0=dS_{sys}-dE_{sys}/T.$ Hence the condition for equilibrium is $0=d(E_{sys}-TS_{sys})=-X_{sys}.$

zero. A review of the calculation above shows that the no go result (6) obtains no matter what the temperature, even if it close to absolute zero.⁴

2.2 What It Takes to Beat Fluctuations

If fluctuations obliterate thermodynamically reversible processes, how is it possible for these processes to figure in thermodynamic analysis at all? The answer is that the disequilibrium required to overcome fluctuations is negligible macroscopically. While the no go result applies to macroscopic systems, it is overcome by disequilibria too small to trouble us. However, at the molecular scale explored by the thermodynamics of computation, the situation is reversed. There, the disequilibria needed to overcome fluctuations dominate. Most importantly, it requires thermodynamic entropy creation in amounts that well exceed those tracked by Landauer's principle.

A few computations illustrate this answer. Relation (4) tells us that we can probabilistically favor the end stage λ_2 over the initial stage λ_1 if the end stage free energy $F(\lambda_2)$ is smaller than the initial stage free energy $F(\lambda_1)$. A decrease of 3kT is sufficient for a modest favoring in the ratio of 20:1, for then

$$p(\lambda_2)/p(\lambda_1) = \exp(-(-3kT)/kT) = \exp(3) = 20$$

The dissipation associated with the reduction in free energy $F(\lambda_2)$ - $F(\lambda_1)$ = -3kT is a minimum increase in the thermodynamic entropy of⁵

$$S(\lambda_2)$$
 - $S(\lambda_1)$ - $(E(\lambda_2)$ - $E(\lambda_1))/T = 3k$

We have $\Delta S_{sys} = S(\lambda_2)$ - $S(\lambda_1)$. By conservation of energy, - $(E(\lambda_2)$ - $E(\lambda_1)$) is the energy gained by the environment. By supposition, this energy is passed by heat transfer only. In the least dissipative case of a thermodynamically reversible heat transfer that corresponds to the minimum increase of entropy $\Delta S_{env} = -(E(\lambda_2) - E(\lambda_1))/T$.

⁴ Temperature does affect the free energy needed to override the fluctuations. We see below that a probabilistic favoring of 20:1 is achieved by a free energy reduction of 3kT. This reduction diminishes as T decreases. However the thermodynamic entropy created remains at least 3k, independent of the temperature.

⁵ To see this, use F=E-TS to rewrite $F(\lambda_2)$ - $F(\lambda_1)$ = -3kT as

$$\Delta S_{tot} = \Delta S_{sys} + \Delta S_{env} = 3k$$

where the change Δ is applied to the entropy of the universe as a whole S_{tot} , which is the sum of the system entropy S_{sys} and the environment entropy S_{env} . Even though this modest probabilistic favoring by no means assures completion of the process, the entropy creation of at least 3k is many times greater than the $k \ln 2 = 0.69k$ of entropy tracked by Landauer's principle in a single bit erasure.

Since the ratio of probability densities grows exponentially with free energy differences in (4), further creation of thermodynamic entropy can bring probability density ratios that strongly favor completion of the process. For example, if we increase the free energy difference to 25kT, then the end stage is strongly favored, for

$$p(\lambda_2)/p(\lambda_1) = \exp(-(-25kT)/kT) = \exp(25) = 7.2 \times 10^{10}$$
.

In macroscopic terms, however, 25kT of free energy is negligible. This quantity, 25kT, is the mean thermal energy of ten diatomic molecules, such as ten oxygen molecules. Hence, there is no obstacle to introducing a slight disequilibrium in a macroscopic system in order to nudge a thermodynamically reversible process to completion.

3. Illustrations of the No Go Result for a One-Molecule Gas

This no go result applies to all thermodynamically reversible processes in systems in thermal equilibrium with their environment. However its derivation and its statement as (6) is remote from its implementation in specific systems. It is helpful to illustrate how fluctuations obliterate a simple process described in the thermodynamics of computation, the thermodynamically reversible, isothermal expansion and compression of a one-molecule gas. The analysis of the last section provides the precise computation. Here I give simpler estimates of the disturbing effects of fluctuations.

3.1 Reversible, Isothermal Expansion and Compression

A monatomic one-molecule gas is confined to a vertically oriented cylinder and the gas pressure is contained by the weight of the piston. The process intended is a thermodynamically reversible, isothermal expansion or compression of the gas. Our expectation is that this process will proceed indefinitely slowly, with the weight of the piston maintained just minutely away

from the equilibrium weight so that the expansion or compression is only just favored. As the piston is raised in an expansion, it draws work energy from the one-molecule gas; and this energy is restored to the one-molecule gas as heat from the environment. The gas exerts a pressure P=kT/V, for V the volume of the gas. Thus the work extracted in a doubling of the volume and thus also the heat passed to the gas is given by $\int_{V}^{2V} kT/V' dV' = kT \ln 2$. The thermodynamic entropy change in the gas is the familiar k ln 2.

That is our expectation. It is confounded by fluctuations. Consider the piston first. It is a thermal system that is Boltzmann distributed over its height $h \ge 0$ above the piston floor according to

$$p(h) = (Mg/kT) \exp(-Mgh/kT)$$

where M is the piston mass. The mean of this distribution is kT/Mg and its standard deviation is also kT/Mg.

This latter number measures the extent of thermal fluctuations in the height of the piston. For a macroscopic piston, M will be very much larger than kT/g and the extent of fluctuations in height will be negligible. However in this case of a one-molecule gas, the piston must be very light if it is to be suspended at equilibrium by the pressure of the one-molecule gas. Hence its M is small and the fluctuations in height will be great. They can be estimated quantitatively as follows. The weight of the piston is Mg. The mean force exerted by the gas pressure is (kT/V).A = kT/h, where A is the area of the piston and h its height above the base of the cylinder, so that V = Ah. Setting these two forces equal as the condition for equilibrium, we recover the equilibrium height as⁶

$$h_{eq} = kT/Mg$$

Remarkably, this quantity h_{eq} is just the same as the mean height and standard deviation of the above distribution, both of which are also given by kT/Mg.

⁶ Hence the mean energy of height is $Mgh_{eq} = kT$. While this energy is associated with a single degree of freedom of the moving piston, it differs from the familiar equipartition mean energy per degree of freedom (1/2)kT, because the relevant term of the piston's Hamiltonian, Mgh, is linear in h and not quadratic, as the equipartition theorem assumes.

This extraordinary result can be expressed more picturesquely as follows. If we set up the piston so that its weight perfectly balances the mean pressure force of the one-molecule gas, it will not remain at the equilibrium height, but will fluctuate immediately through the entire volume of the gas. It will perhaps be suddenly flung skyward by a collision with molecule; and it may then fall precipitously between collisions. The intended process of a gentle, indefinitely slow expansion or contraction is lost completely behind the wild gyrations of the piston over the full volume of the one-molecule gas.

Similar results hold for heat transfer between the one-molecule gas and its environment. Since it is monatomic, the Boltzmann distribution of the gas energy E is

$$p(E) = 2(E/\pi)^{1/2} (kT)^{-3/2} \exp(-E/kT)$$

The mean of this distribution is the familiar equipartition energy (3/2) kT and the standard deviation is $(3/2)^{1/2}$ kT = 1.225 kT.⁷ Hence, simply by virtue of its contact with the environment at temperature T, the one-molecule gas energy will be swinging wildly through a range comparable in size to the total mean energy of the gas.

We had expected that we would track a quantity of heat $kT \ln 2 = 0.69 kT$ while the piston slowly and gently moves to halve or double the volume of the gas. What we find is that the piston is wildly and randomly flung to and fro through the entire volume of the gas, while the gas energy fluctuates similarly wildly over a range greater than the 0.69 kT of heat transfer we track. We had expected a process that proceeds calmly at arbitrarily slow speed from start to finish. Instead we find a chaos of wild gyrations with no discernible start or finish.

This is a rough analysis. To maintain the equilibrium of a thermodynamically reversible process would require that the weight Mg be adjusted as the volume V changes since the gas pressure will vary inversely with volume. Norton (2011, Section 7.5) replaces the uniform force field of gravity with another force field that varies with height in precisely the way needed to maintain mean quantities at equilibrium.

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⁷ This and the earlier energy standard deviation can be computed most rapidly from Einstein's energy fluctuation theorem, which identifies the variance of the energy with kT^2 d<E>/dT, where <E> is the mean energy. For the piston, <E>=kT, so the variance is $(kT)^2 = (Mgh_{eq})^2$. For the monatomic gas, <E>=(3/2)kT, so the variance is $(3/2)(kT)^2$. The standard deviation is the square root of the variance.

3.2 Generality

A one-molecule gas confined in a cylinder by a piston is fanciful and cannot be realized practically. It is, however, one of the most discussed examples in the thermodynamics of computation because it is easy to visualize. Its statistical and thermodynamic properties mimic those of more realistic systems with few degrees of freedom. We may model a memory device as a two-chambered cell with a single molecule trapped in one part. A more realistic implementation of the memory device is a single electric charge trapped by a potential well in a solid state medium; or a magnetic dipole aligned into a specific orientation by a magnetic field.

The thermodynamic operations carried out on the one-molecule gas have analogs in the more realistic implementations. Mechanical variables such as volume and pressure are replaced by electric and magnetic correlates. The general results remain the same. If we halve the range of possible states of a memory device, we reduce its thermodynamic entropy by k ln 2, just as we do when we halve the volume of a one-molecule gas. The large fluctuations exhibited by the one-molecule gas derive from its small number of degrees of freedom. Correspondingly, the more realistic implementations will exhibit similarly large fluctuations.

The two processes investigated were heating/cooling and expansion/contraction of the gas. These are instances of the two processes that appear in all thermodynamically reversible processes: heat transfer and exchange of generalized work energy. As a result, the analysis here has a quite broad scope. Consider thermodynamically reversible measurement, in which one device reads the state of another. For example, a magnetic dipole reads the state of a second dipole when the two slowly approach and align in a process that maintains equilibrium throughout. This detection or measurement process is a reversible compression of the phase space of the reader dipole and is thermodynamically analogous to compression of a one-molecule gas. As a result, this measurement process will be fatally disrupted by fluctuations. While a standard claim of the thermodynamics literature is that these measurements can be performed without dissipation, the no go result shows that dissipation is required if the fluctuations are to be overcome and the process driven to a correct reading.

4. A Loophole?

Each computation consists of many steps. Dissipation, significant at the molecular level, is required by the no go result to bring each of these steps to completion. Bennett (1973, 1982) proposes an ingenious loophole for computations with very many steps. The very many thermodynamically reversible steps are chained together to form one large thermodynamically reversible process. The computer's state wanders back and forth through the various stages in a generalization of Brownian motion. The no go result affirms that the state will be uniformly distributed over all the stages of the computation. Bennett now makes the step to the final state highly dissipative, so that it can be favored with arbitrarily high probability. Hence the computation will eventually terminate in this final state with high probability. The thermodynamic entropy created in this final, irreversible step may be large. However, if there are very many steps combined into the overall computation, the entropy created per step can be quite small.

Whether this loophole can succeed depends on whether the many steps of a computation can be chained together in such a way that achieving the final state also assures that all the computer's components are in the intended final states. The danger point is when the computer completes one step and initiates the next. The initiation of the second step must arise only when the first step is completed and the state of the computer conforms to what the logical specification of the program requires for that first step. We need to be assured that the disrupting effects of fluctuations will not trigger the second step before these conditions are met.

In an attempt to assure this, Bennett (1982) describes a Brownian clockwork computer, a mechanical implementation of a Turing machine. Its parts are mechanically interlocked so that when the tape manipulator head reaches its final state, each of the cells of the tape are in the final states intended by the logical specification of the computation.

Bennett's description of the device is detailed with vivid line drawings. However it is incomplete in the one aspect that matters most. The statistical mechanical properties of the individual components are poorly represented. Here is the easiest way to see that they are omitted: the machine is sufficiently powerful that we could set it up with a large tape carrying

"random" data of 0s and 1s and then run an erasure program that resets all the cells to zero.⁸ On Bennett's view, there must be an associated creation of thermodynamic entropy of at least k ln 2 per bit erased and the passing of kT ln 2 of heat per bit erased to the environment. Yet their creation is nowhere apparent in the operation of the machine.⁹

The narrative that describes the machine's operation depends on our imagining processes that are unproblematic if implemented by macroscopic bodies. For example, the branching of the program's execution arises when the path of the manipulator is obstructed by a knob whose position encodes the data recorded in the tape cell. Our macroscopic intuitions preclude the manipulator ever proceeding with a misread of the data. These same processes may fail if we attempt to implement them in a thermodynamically reversible manner at the molecular level. For that means that all interactions must be at equilibrium. The components at issue, such as a single molecule or a molecular-scale dipole, exert very weak forces on average and these forces are confounded by fluctuations comparable in size to the average. Another component interacting with them can only apply correspondingly weak forces, else the requirement of equilibrium of thermodynamic reversibility would be violated. Once again our intended average behavior would be immersed in wild fluctuations. The resulting interaction would be very different from a macroscopically pictured manipulator thumping into macroscopic knob and being definitively obstructed by it.

The following indicates how adding these thermal complications would compromise the operation of the clockwork computer. The obstruction of the manipulator head by the data knob is equivalent to the reading by a detector of the state of a data cell. The manipulator in effect reads the state of the data cell and records the reading by implementing one of several possible computational paths. Bennett (1982, pp. 307-308; 1987, p.14) has described two schemes in which a reader detects the position of a single component memory device in a reversible thermodynamic process. The molecular implementation is quite fragile in comparison with its robust macroscopic counterpart and fails precisely because the analysis of both schemes neglects

⁸ The program reads a cell and rewrites its contents to 0, if the cell has a 1. If the cell has a 0, it moves one cell to the right and repeats.

⁹ Or one could assume that the physical description is complete so that the machine can erase the tape without thermodynamic entropy creation. That contradicts Landauer's principle.

how fluctuations confound the intended behavior of thermodynamically reversible processes at the molecular scale. Norton (2011, §7.3) describes how both detection schemes fail. For the case of binary data, they are as likely as not to terminate with the detector reading the right as the wrong result.

We have every reason to expect that these problems would appear were the clockwork, Brownian computer somehow implemented with molecular scale storage devices and operated by thermodynamically reversible processes. We have no assurance that any step would proceed according to its logical specification. If the reading of data in a cell is implemented as Bennett describes, they would likely as not return the wrong result. When the manipulator is eventually trapped probabilistically in its final state, we should expect the tape to be left in a state of chaos that does not reflect the results intended by the logical specification of the program.

In short, the loophole fails. It is a conjecture, motivated by macroscopic intuitions that do not apply at molecular scales.

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